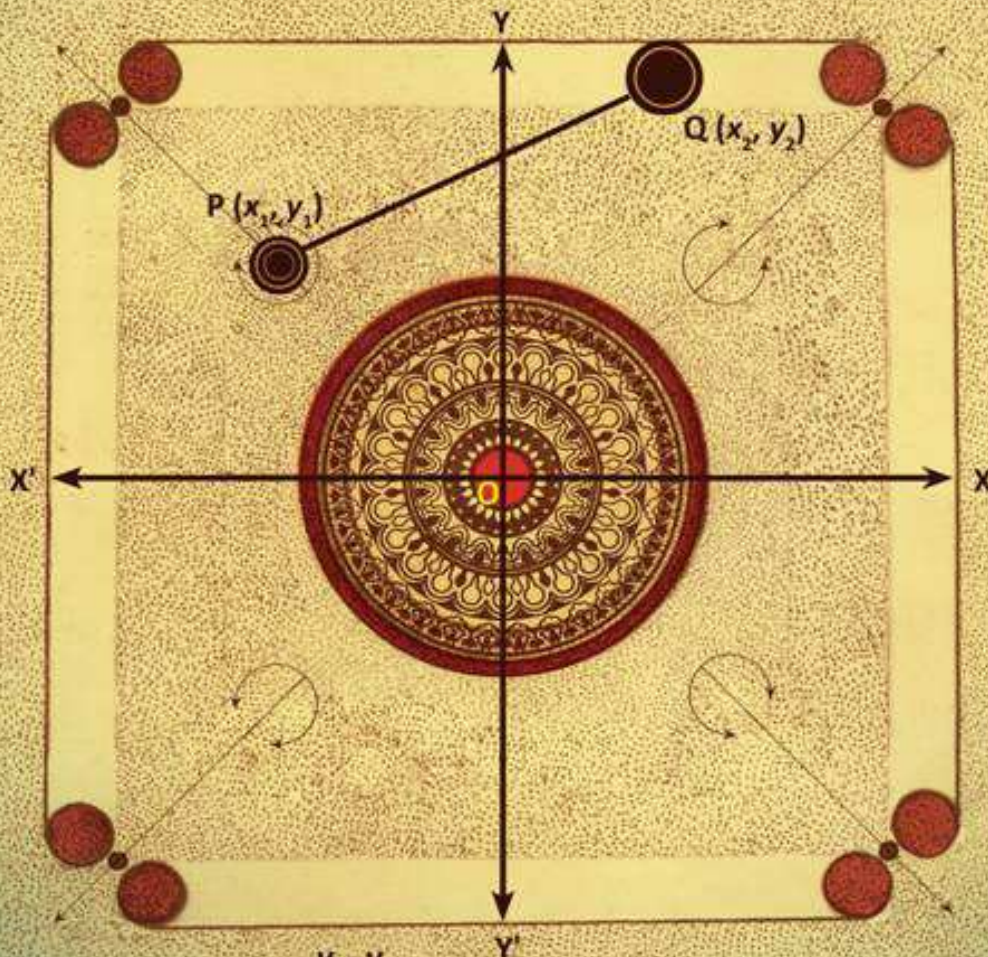


MATHEMATICS - II



# GOMETRY

BASED ON MAHARASHTRA STATE BOARD SYLLABUS



$$\text{Slope of PQ} = \frac{y_2 - y_1}{x_2 - x_1}$$

**STD. X**

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**Target** Publications Pvt. Ltd.

# STD. X

## Mathematics II

# Geometry

Sixth Edition: March 2016

### Salient Features

- Written as per the new textbook.
- Exhaustive coverage of entire syllabus.
- Topic-wise distribution of all textual questions and practice problems at the beginning of every chapter
- Covers solutions to all textual exercises and problem set.
- Includes additional problems for practice.
- Indicative marks for all problems.
- Comprehensive solution to Question Bank.
- Constructions drawn with accurate measurements.
- Includes Board Question Papers of 2014, 2015 and March 2016.

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## Preface

Geometry is the mathematics of properties, measurement and relationships of points, lines, angles, surfaces and solids. It is widely used in the fields of science, engineering, computers, architecture etc. It is a vast subject dealing with the study of properties, definitions, theorems, areas, perimeter, angles, triangles, mensuration, co-ordinates, constructions etc.

The study of Geometry requires a deep and intrinsic understanding of concepts. Hence, to ease this task, we bring to you “**Std. X: Geometry**”, a complete and thorough guide critically analysed and extensively drafted to boost the confidence of the students. The question answer format of this book helps the student to understand and grasp each and every concept thoroughly. The book is based on the new text book and covers the entire syllabus. At the beginning of every chapter, topic-wise distribution of all textual questions and practice problems has been provided for simpler understanding of different types of questions. The book contains answers to textual exercises, problems sets and Question bank. It also includes additional questions for practice. All the diagrams are neat and have proper labelling. The book has a unique feature that all the constructions are as per the scale. Another feature of the book is its layout which is attractive and inspires the student to read.

Marks are provided for each and every problem. However, marks mentioned are indicative and are subject to change as per Maharashtra State Board’s discretion.

There is always room for improvement and hence we welcome all suggestions and regret any errors that may have occurred in the making of this book.

*A book affects eternity; one can never tell where its influence stops.*

*Best of luck to all the aspirants!*

Yours’ faithfully,

Publisher

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## MARKING SCHEME

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### Marking Scheme (for March 2014 exam and onwards)

#### Written Exam

|                       |                  |              |
|-----------------------|------------------|--------------|
| Algebra               | 40 Marks         | Time: 2 hrs. |
| Geometry              | 40 Marks         | Time: 2 hrs. |
| * Internal Assessment | 20 Marks         |              |
| <b>Total</b>          | <b>100 Marks</b> |              |

#### \* Internal Assessment

|                                   |          |   |
|-----------------------------------|----------|---|
| Home Assignment:                  | 10 Marks | 5-5 Home assignment for Algebra and Geometry of 10 marks each would be given. Marks obtained out of 100 would be converted to marks out of 10.  |
| Test of multiple choice question: | 10 Marks | Depending upon the entire syllabus, internal test for Algebra and Geometry with 20 marks each would be taken at the end of second semester. Marks obtained out of 40 would be converted to marks out of 10. |

|              |                 |
|--------------|-----------------|
| <b>Total</b> | <b>20 marks</b> |
|--------------|-----------------|

## ALGEBRA AND GEOMETRY

### Mark Wise Distribution of Questions

|  | Marks     | Marks with Option |
|--|-----------|-------------------|
| 6 sub questions of 1 mark each: Attempt any 5  | 05        | 06                |
| 6 sub questions of 2 marks each: Attempt any 4 | 08        | 12                |
| 5 sub questions of 3 marks each: Attempt any 3 | 09        | 15                |
| 3 sub questions of 4 marks each: Attempt any 2 | 08        | 12                |
| 3 sub questions of 5 marks each: Attempt any 2 | 10        | 15                |
| <b>Total:</b>                                  | <b>40</b> | <b>60</b>         |

### Weightage to Types of Questions

| Sr. No. | Type of Questions | Marks     | Percentage of Marks |
|---------|-------------------|-----------|---------------------|
| 1.      | Very short answer | 06        | 10                  |
| 2.      | Short answer      | 27        | 45                  |
| 3.      | Long answer       | 27        | 45                  |
|         | <b>Total:</b>     | <b>60</b> | <b>100</b>          |

### Weightage to Objectives

| Sr. No | Objectives    | Algebra Percentage marks | Geometry Percentage marks |
|--------|---------------|--------------------------|---------------------------|
| 1.     | Knowledge     | 15                       | 15                        |
| 2.     | Understanding | 15                       | 15                        |
| 3.     | Application   | 60                       | 50                        |
| 4.     | Skill         | 10                       | 20                        |
|        | <b>Total:</b> | <b>100</b>               | <b>100</b>                |

### Unit wise Distribution: Algebra

| Sr. No. | Unit                             | Marks with option |
|---------|----------------------------------|-------------------|
| 1.      | Arithmetic Progression           | 12                |
| 2.      | Quadratic equations              | 12                |
| 3.      | Linear equation in two variables | 12                |
| 4.      | Probability                      | 10                |
| 5.      | Statistics – I                   | 06                |
| 6.      | Statistics – II                  | 08                |
|         | <b>Total:</b>                    | <b>60</b>         |

### Unit wise Distribution: Geometry

| Sr. No. | Unit                    | Marks with option |
|---------|-------------------------|-------------------|
| 1.      | Similarity              | 12                |
| 2.      | Circle                  | 10                |
| 3.      | Geometric Constructions | 10                |
| 4.      | Trigonometry            | 10                |
| 5.      | Co-ordinate Geometry    | 08                |
| 6.      | Mensuration             | 10                |
|         | <b>Total:</b>           | <b>60</b>         |

# Contents

| Sr. No. | Topic Name                          | Page No. |
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| 4       | Trigonometry                        | 142      |
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# 01 Similarity

| Type of Problems   | Exercise                                     | Q. Nos.  |
|--|--|--|
| Properties of the Ratios of Areas of Two Triangles   | 1.1  | Q.1, 2, 3, 4, 5, 6, 7                              |
|  | Practice Problems<br>(Based on Exercise 1.1) | Q.1, 2, 3  |
|  | Problem set-1                                | Q.7 (iii.), 20                                     |
| Basic Proportionality Theorem (B.P.T.) and Converse of B.P.T.  | 1.2  | Q.1, 2, 6, 10                                      |
|  | Practice Problems<br>(Based on Exercise 1.2) | Q.4, 5, 6, 10                                      |
|  | Problem set-1                                | Q.6 (i.), 15, 18, 19, 21                           |
| Application of BPT (Property of Intercept made by Three Parallel lines on a Transversal and/or Property of an Angle Bisector of a Triangle)  | 1.2  | Q.3, 4, 5, 7, 9                                    |
|  | Practice Problems<br>(Based on Exercise 1.2) | Q.7, 8, 9  |
|  | Problem set-1                                | Q.16, 22   |
| Similarity of Triangles  | 1.2  | Q.8  |
|  | 1.3  | Q.1, 2, 3, 4, 5, 6                                 |
|  | Practice Problems<br>(Based on Exercise 1.3) | Q.11, 12, 13, 14, 15                               |
|  | Problem set-1                                | Q.1, 2, 4 (i., ii.), 7 (i., ii.), 8, 9, 10, 24, 25 |
| Areas of Similar Triangles   | 1.4  | Q.1, 2, 3, 4, 5, 6                                 |
|  | Practice Problems<br>(Based on Exercise 1.4) | Q.16, 17, 18, 19, 20                               |
|  | Problem set-1                                | Q.3, 4(iii.), 5, 6(ii., iii.), 17, 23              |
| Similarity in Right Angled Triangles and Property of Geometric Mean  | 1.5  | Q.2, 6 (i.)  |
|  | Practice Problems<br>(Based on Exercise 1.5) | Q.22   |
|  | 1.7  | Q.4  |
| Pythagoras Theorem and Converse of Pythagoras Theorem  | 1.5  | Q.1, 3, 4, 5, 6(ii.), 7, 8                         |
|  | Practice Problems<br>(Based on Exercise 1.5) | Q.21, 23, 24, 25                                   |
|  | 1.6  | Q.2, 4   |
|  | Problem set-1                                | Q.11, 12   |
| Theorem of $30^\circ$ - $60^\circ$ - $90^\circ$ Triangle, Converse of $30^\circ$ - $60^\circ$ - $90^\circ$ Triangle Theorem and Theorem of $45^\circ$ - $45^\circ$ - $90^\circ$ Triangle | 1.6  | Q.1, 3, 5, 6, 7                                    |
|  | Practice Problems<br>(Based on Exercise 1.6) | Q.26, 27, 28, 29                                   |
| Applications of Pythagoras Theorem   | 1.7  | Q.5  |
| Apollonius Theorem   | 1.7  | Q.1, 2, 3, 6                                       |
|  | Practice Problems<br>(Based on Exercise 1.7) | Q.30, 31, 32                                       |
|  | Problem set-1                                | Q.13, 14   |

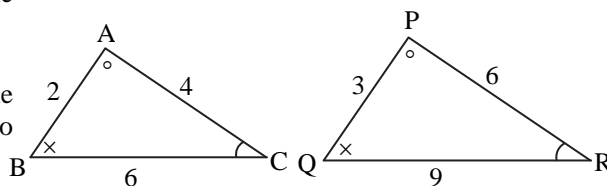


**Concepts of Std. IX**

**Similarity of triangles**

For a given one-to-one correspondence between the vertices of two triangles, if

- i. their corresponding angles are congruent and
- ii. their corresponding sides are in proportion then the correspondence is known as similarity and the two triangles are said to be similar.



In the figure, for correspondence  $ABC \leftrightarrow PQR$ ,

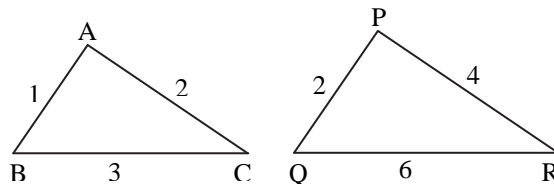
- i.  $\angle A \cong \angle P, \angle B \cong \angle Q, \angle C \cong \angle R$
- ii.  $\frac{AB}{PQ} = \frac{2}{3}, \frac{BC}{QR} = \frac{6}{9} = \frac{2}{3}, \frac{AC}{PR} = \frac{4}{6} = \frac{2}{3}$   
 i.e.,  $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$

Hence,  $\triangle ABC$  and  $\triangle PQR$  are similar triangles and are symbolically written as  $\triangle ABC \sim \triangle PQR$ .

**Test of similarity of triangles**

**1. S–S–S test of similarity:**

For a given one-to-one correspondence between the vertices of two triangles, the two triangles are similar if the sides of one triangle are proportional to the corresponding sides of the other triangle.



In the figure,

$$\frac{AB}{PQ} = \frac{1}{2}, \frac{BC}{QR} = \frac{3}{6} = \frac{1}{2}, \frac{AC}{PR} = \frac{2}{4} = \frac{1}{2}$$

$$\therefore \frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$$

$$\therefore \triangle ABC \sim \triangle PQR$$

---- [By S–S–S test of similarity]

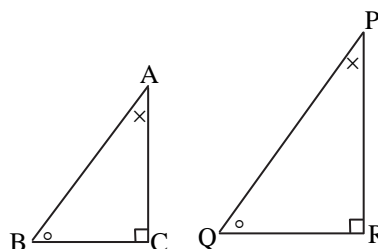
**2. A–A–A test of similarity [A–A test]:**

For a given one-to-one correspondence between the vertices of two triangles, the two triangles are similar if the angles of one triangle are congruent to the corresponding angles of the other triangle.

In the figure,

$$\text{if } \angle A \cong \angle P, \angle B \cong \angle Q, \angle C \cong \angle R$$

$$\text{then } \triangle ABC \sim \triangle PQR$$



---- [By A–A–A test of similarity]

**Note:** A–A–A test is verified same as A–A test of similarity.

**3. S–A–S test of similarity:**

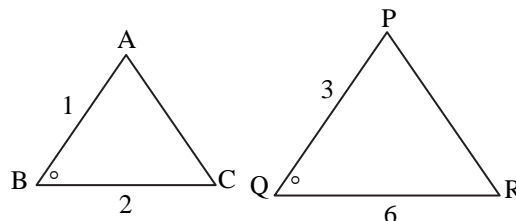
For a given one-to-one correspondence between the vertices of two triangles, the two triangles are similar if two sides of a triangle are proportional to the two corresponding sides of the other triangle and the corresponding included angles are also congruent.

In the figure,

$$\frac{AB}{PQ} = \frac{1}{3}, \frac{BC}{QR} = \frac{2}{6} = \frac{1}{3}$$

$$\therefore \frac{AB}{PQ} = \frac{BC}{QR} \text{ and } \angle B \cong \angle Q$$

$$\therefore \triangle ABC \sim \triangle PQR$$



---- [By S–A–S test of similarity]

**Converse of the test for similarity:****i. Converse of S–S–S test:**

If two triangles are similar, then the corresponding sides are in proportion.

If  $\triangle ABC \sim \triangle PQR$  then,

$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR} \quad \text{---- [Corresponding sides of similar triangles]}$$

**ii. Converse of A–A–A test:**

If two triangles are similar, then the corresponding angles are congruent.

If  $\triangle ABC \sim \triangle PQR$ ,

then  $\angle A \cong \angle P$ ,  $\angle B \cong \angle Q$  and  $\angle C \cong \angle R$  ---- [Corresponding angles of similar triangles]

**Note:** ‘Corresponding angles of similar triangles’ can also be written as c.a.s.t.

‘Corresponding sides of similar triangles’ can also be written as c.s.s.t.

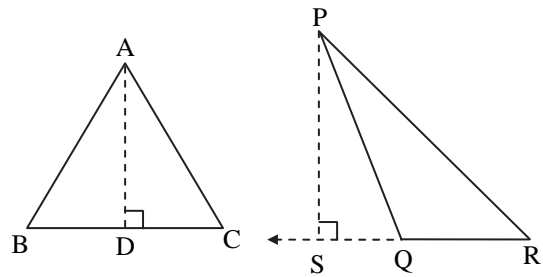
**1.1 Properties of the ratios of areas of two triangles****Property – I**

**The ratio of areas of two triangles is equal to the ratio of the product of their bases and corresponding heights.**

[2 marks]

**Given:** In  $\triangle ABC$  and  $\triangle PQR$ , seg  $AD \perp$  seg  $BC$ , B–D–C,  
seg  $PS \perp$  ray  $RQ$ , S–Q–R

**To prove that:**  $\frac{A(\triangle ABC)}{A(\triangle PQR)} = \frac{BC \times AD}{QR \times PS}$



**Proof:**

$$A(\triangle ABC) = \frac{1}{2} \times BC \times AD \quad \text{---- (i)}$$

$$A(\triangle PQR) = \frac{1}{2} \times QR \times PS \quad \text{---- (ii)}$$

} [Area of a triangle =  $\frac{1}{2} \times$  base  $\times$  height]

Dividing (i) by (ii), we get

$$\frac{A(\triangle ABC)}{A(\triangle PQR)} = \frac{\frac{1}{2} \times BC \times AD}{\frac{1}{2} \times QR \times PS}$$

$$\therefore \frac{A(\triangle ABC)}{A(\triangle PQR)} = \frac{BC \times AD}{QR \times PS}$$

**For Understanding****When do you say the triangles have equal heights?**

We can discuss this in three cases.

**Case – I**

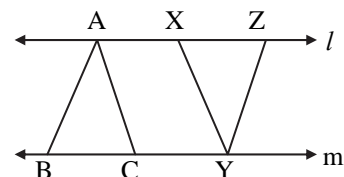
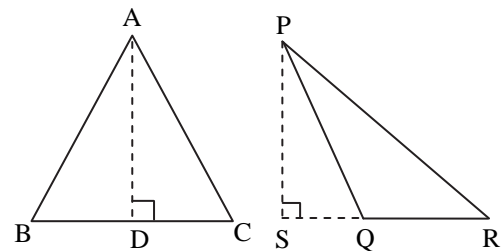
In the adjoining figure,

segments  $AD$  and  $PS$  are the corresponding heights of  $\triangle ABC$  and  $\triangle PQR$  respectively.

If  $AD = PS$ , then  $\triangle ABC$  and  $\triangle PQR$  are said to have equal heights.

**Case – II**

In the adjoining figure,  $\triangle ABC$  and  $\triangle XYZ$  have their one vertex on one of the parallel lines and the other two vertices lie on the other parallel line. Hence the two triangles are said to lie between the same parallel lines and are said to have equal heights.

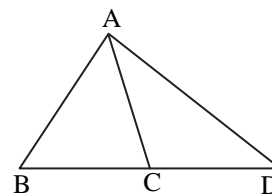






**Case – III**

In the adjoining figure,  $\triangle ABC$ ,  $\triangle ACD$  and  $\triangle ABD$  have a common vertex A and the sides opposite to vertex A namely, BC, CD and BD respectively of these triangles lie on the same line. Hence,  $\triangle ABC$ ,  $\triangle ACD$  and  $\triangle ABD$  are said to have equal heights and BC, CD and BD are their respective bases.



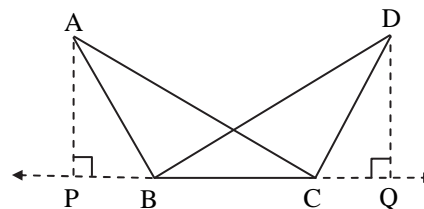
**Property – II**

**The ratio of areas of two triangles having equal base is equal to the ratio of their corresponding heights.**

**Example:**

$\triangle ABC$  and  $\triangle DCB$  have a common base BC.

$$\therefore \frac{A(\triangle ABC)}{A(\triangle DCB)} = \frac{AP}{DQ}$$



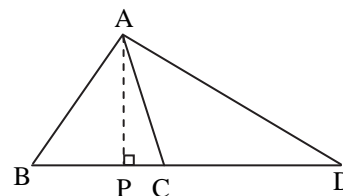
**Property – III**

**The ratio of areas of two triangles having equal height is equal to the ratio of their corresponding bases.**

**Example:**

$\triangle ABC$ ,  $\triangle ACD$  and  $\triangle ABD$  have a common vertex A and their sides opposite to vertex A namely, BC, CD, BD respectively lie on the same line. Hence they have equal heights. Here, AP is common height.

$$\therefore \frac{A(\triangle ABC)}{A(\triangle ACD)} = \frac{BC}{CD}, \frac{A(\triangle ABC)}{A(\triangle ABD)} = \frac{BC}{BD}, \frac{A(\triangle ACD)}{A(\triangle ABD)} = \frac{CD}{BD}$$



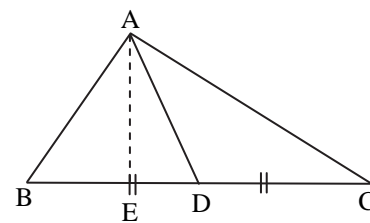
**Property – IV**

**Areas of two triangles having equal bases and equal heights are equal.**

**Example:**

$\triangle ABD$  and  $\triangle ACD$  have a common vertex A and their sides opposite to vertex A namely, BD and DC respectively lie on the same line. Hence the triangles have equal heights. Also their bases BD and DC are equal.

$$\therefore A(\triangle ABD) = A(\triangle ACD)$$



**Exercise 1.1**

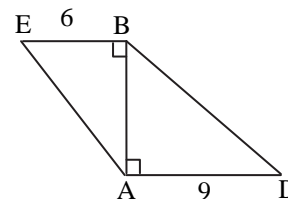
- In the adjoining figure, seg  $BE \perp$  seg AB and seg  $BA \perp$  seg AD.  
If  $BE = 6$  and  $AD = 9$ , find  $\frac{A(\triangle ABE)}{A(\triangle BAD)}$ . [Oct 14, July 15] [1 mark]

**Solution:**

$$\frac{A(\triangle ABE)}{A(\triangle BAD)} = \frac{BE}{AD} \quad \text{--- [Ratio of areas of two triangles having equal base is equal to the ratio of their corresponding heights.]}$$

$$\therefore \frac{A(\triangle ABE)}{A(\triangle BAD)} = \frac{6}{9}$$

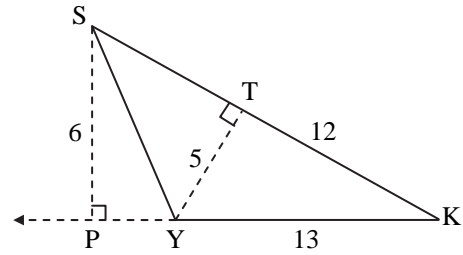
$$\therefore \frac{A(\triangle ABE)}{A(\triangle BAD)} = \frac{2}{3}$$





2. In the adjoining figure, seg  $SP \perp$  side  $YK$  and seg  $YT \perp$  seg  $SK$ . If  $SP = 6$ ,  $YK = 13$ ,  $YT = 5$  and  $TK = 12$ , then find  $A(\Delta SYK) : A(\Delta YTK)$ .

[2 marks]



---- [Ratio of areas of two triangles is equal to the ratio of the product of their bases and corresponding heights.]

**Solution:**

$$\frac{A(\Delta SYK)}{A(\Delta YTK)} = \frac{YK \times SP}{TK \times YT}$$

$$\therefore \frac{A(\Delta SYK)}{A(\Delta YTK)} = \frac{13 \times 6}{12 \times 5}$$

$$\therefore \frac{A(\Delta SYK)}{A(\Delta YTK)} = \frac{13}{10}$$

$$\therefore A(\Delta SYK) : A(\Delta YTK) = 13 : 10$$

3. In the adjoining figure,  $RP : PK = 3 : 2$ , then find the values of the following ratios:

i.  $A(\Delta TRP) : A(\Delta TPK)$

ii.  $A(\Delta TRK) : A(\Delta TPK)$

iii.  $A(\Delta TRP) : A(\Delta TRK)$

[Mar 14] [3 marks]

**Solution:**

$$RP : PK = 3 : 2$$

Let the common multiple be  $x$ .

$$\therefore RP = 3x, PK = 2x$$

$$RK = RP + PK$$

$$\therefore RK = 3x + 2x$$

$$\therefore RK = 5x$$

$$i. \frac{A(\Delta TRP)}{A(\Delta TPK)} = \frac{RP}{PK}$$

$$\therefore \frac{A(\Delta TRP)}{A(\Delta TPK)} = \frac{3x}{2x}$$

$$\therefore \frac{A(\Delta TRP)}{A(\Delta TPK)} = \frac{3}{2}$$

$$\therefore A(\Delta TRP) : A(\Delta TPK) = 3 : 2$$

---- [Given]

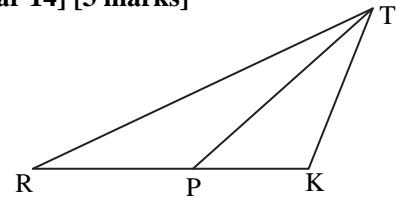
---- (i)

---- [R-P-K]

---- (ii)

---- [Ratio of the areas of two triangles having equal heights is equal to the ratio of their corresponding bases.]

---- [From (i)]



$$ii. \frac{A(\Delta TRK)}{A(\Delta TPK)} = \frac{RK}{PK}$$

---- [Ratio of the areas of two triangles having equal heights is equal to the ratio of their corresponding bases.]

$$\therefore \frac{A(\Delta TRK)}{A(\Delta TPK)} = \frac{5x}{2x}$$

---- [From (i) and (ii)]

$$\therefore \frac{A(\Delta TRK)}{A(\Delta TPK)} = \frac{5}{2}$$

$$\therefore A(\Delta TRK) : A(\Delta TPK) = 5 : 2$$

$$iii. \frac{A(\Delta TRP)}{A(\Delta TRK)} = \frac{RP}{RK}$$

---- [Ratio of the areas of two triangles having equal heights is equal to the ratio of their corresponding bases.]

$$\therefore \frac{A(\Delta TRP)}{A(\Delta TRK)} = \frac{3x}{5x}$$

---- [From (i) and (ii)]

$$\therefore \frac{A(\Delta TRP)}{A(\Delta TRK)} = \frac{3}{5}$$

$$\therefore A(\Delta TRP) : A(\Delta TRK) = 3 : 5$$



4. The ratio of the areas of two triangles with the common base is 6 : 5. Height of the larger triangle is 9 cm. Then find the corresponding height of the smaller triangle. [Mar 15] [3 marks]

**Solution:**

Let  $A_1$  and  $A_2$  be the areas of larger triangle and smaller triangle respectively and  $h_1$  and  $h_2$  be their corresponding heights.

$$\frac{A_1}{A_2} = \frac{6}{5} \quad \text{---- (i) [Given]}$$

$$h_1 = 9 \quad \text{---- (ii) [Given]}$$

$$\frac{A_1}{A_2} = \frac{h_1}{h_2} \quad \text{---- [Ratio of the areas of two triangles having equal base is equal to the ratio of their corresponding heights.]}$$

$$\therefore \frac{6}{5} = \frac{9}{h_2} \quad \text{---- [From (i) and (ii)]}$$

$$\therefore h_2 = \frac{5 \times 9}{6}$$

$$\therefore h_2 = \frac{15}{2}$$

$$\therefore h_2 = 7.5 \text{ cm}$$

$\therefore$  The corresponding height of the smaller triangle is 7.5 cm.

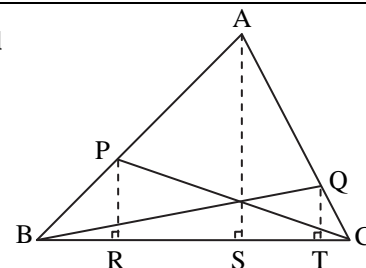
5. In the adjoining figure, seg  $PR \perp$  seg  $BC$ , seg  $AS \perp$  seg  $BC$  and seg  $QT \perp$  seg  $BC$ . Find the following ratios: [3 marks]

i.  $\frac{A(\triangle ABC)}{A(\triangle PBC)}$

ii.  $\frac{A(\triangle ABS)}{A(\triangle ASC)}$

iii.  $\frac{A(\triangle PRC)}{A(\triangle BQT)}$

iv.  $\frac{A(\triangle BPR)}{A(\triangle CQT)}$



**Solution:**

i.  $\frac{A(\triangle ABC)}{A(\triangle PBC)} = \frac{AS}{PR}$  ---- [Ratio of the areas of two triangles having equal bases is equal to the ratio of their corresponding heights.]

ii.  $\frac{A(\triangle ABS)}{A(\triangle ASC)} = \frac{BS}{SC}$  ---- [Ratio of the areas of two triangles having equal heights is equal to the ratio of their corresponding bases.]

iii.  $\frac{A(\triangle PRC)}{A(\triangle BQT)} = \frac{RC \times PR}{BT \times QT}$  ---- [Ratio of the areas of two triangles is equal to the ratio of product of their bases and corresponding heights.]

iv.  $\frac{A(\triangle BPR)}{A(\triangle CQT)} = \frac{BR \times PR}{CT \times QT}$  ---- [Ratio of the areas of two triangles is equal to the ratio of product of their bases and corresponding heights.]

6. In the adjoining figure, seg  $DH \perp$  seg  $EF$  and seg  $GK \perp$  seg  $EF$ . If  $DH = 12$  cm,  $GK = 20$  cm and  $A(\triangle DEF) = 300 \text{ cm}^2$ , then find

- i.  $EF$     ii.  $A(\triangle GEF)$     iii.  $A(\square DFGE)$  [3 marks]

**Solution:**

i. Area of triangle =  $\frac{1}{2} \times$  base  $\times$  height

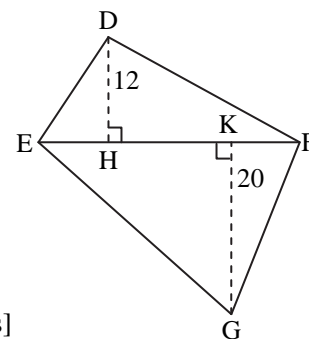
$$\therefore A(\triangle DEF) = \frac{1}{2} \times EF \times DH$$

$$\therefore 300 = \frac{1}{2} \times EF \times 12 \quad \text{---- [Substituting the given values]}$$

$$\therefore 300 = EF \times 6$$

$$\therefore EF = \frac{300}{6}$$

$$\therefore EF = 50 \text{ cm}$$





- ii.  $\frac{A(\triangle DEF)}{A(\triangle GEF)} = \frac{DH}{GK}$  ---- [Ratio of the areas of two triangles having equal bases is equal to the ratio of their corresponding heights.]
- $\therefore \frac{300}{A(\triangle GEF)} = \frac{12}{20}$  ---- [Substituting the given values]
- $\therefore 300 \times 20 = 12 \times A(\triangle GEF)$
- $\therefore \frac{300 \times 20}{12} = A(\triangle GEF)$
- $\therefore A(\triangle GEF) = \frac{300 \times 20}{12}$
- $\therefore A(\triangle GEF) = 500 \text{ cm}^2$  ---- (i)
- 
- iii.  $A(\square DFGE) = A(\triangle DEF) + A(\triangle GEF)$  ---- [Area addition property]
- $\therefore A(\square DFGE) = 300 + 500$  ---- [From (i) and given]
- $\therefore A(\square DFGE) = 800 \text{ cm}^2$

7. In the adjoining figure, seg  $ST \parallel$  side  $QR$ . Find the following ratios. [3 marks]

- i.  $\frac{A(\triangle PST)}{A(\triangle QST)}$       ii.  $\frac{A(\triangle PST)}{A(\triangle RST)}$       iii.  $\frac{A(\triangle QST)}{A(\triangle RST)}$

**Solution:**

- i.  $\frac{A(\triangle PST)}{A(\triangle QST)} = \frac{PS}{QS}$  } [Ratio of the areas of two triangles having equal heights is equal to the ratio of their corresponding bases.]
- ii.  $\frac{A(\triangle PST)}{A(\triangle RST)} = \frac{PT}{TR}$  }

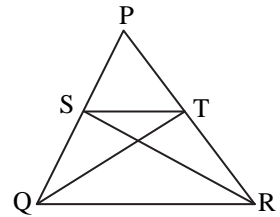
iii.  $\triangle QST$  and  $\triangle RST$  lie between the same parallel lines  $ST$  and  $QR$

$\therefore$  Their heights are equal.

Also  $ST$  is the common base.

$\therefore A(\triangle QST) = A(\triangle RST)$  ---- [Areas of two triangles having common base and equal heights are equal.]

$\therefore \frac{A(\triangle QST)}{A(\triangle RST)} = 1$



## 1.2 Basic Proportionality Theorem (B.P.T)

If a line parallel to a side of a triangle intersects the other sides in two distinct points, then the line divides these sides in proportion. [Mar 14] [4 marks]

**Given:** In  $\triangle PQR$ , line  $l \parallel$  side  $QR$ .

Line  $l$  intersects side  $PQ$  and side  $PR$  in points  $M$  and  $N$  respectively, such that  $P-M-Q$  and  $P-N-R$ .

**To Prove that:**  $\frac{PM}{MQ} = \frac{PN}{NR}$

**Construction:** Draw seg  $QN$  and seg  $RM$ .

**Proof:**

In  $\triangle PMN$  and  $\triangle QMN$ , where  $P-M-Q$ ,

$$\frac{A(\triangle PMN)}{A(\triangle QMN)} = \frac{PM}{MQ}$$

---- (i) [Ratio of the areas of two triangles having equal heights is equal to the ratio of their corresponding bases.]

In  $\triangle PMN$  and  $\triangle RMN$ , where  $P-N-R$ ,

$$\frac{A(\triangle PMN)}{A(\triangle RMN)} = \frac{PN}{NR}$$

---- (ii) [Ratio of the areas of two triangles having equal heights is equal to the ratio of their corresponding bases.]

$$A(\triangle QMN) = A(\triangle RMN)$$

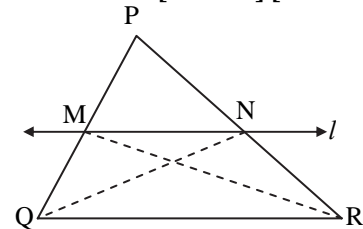
---- (iii) [Areas of two triangles having equal bases and equal heights are equal.]

$$\therefore \frac{A(\triangle PMN)}{A(\triangle QMN)} = \frac{A(\triangle PMN)}{A(\triangle RMN)}$$

---- (iv) [From (i), (ii) and (iii)]

$$\therefore \frac{PM}{MQ} = \frac{PN}{NR}$$

---- [From (i), (ii) and (iv)]

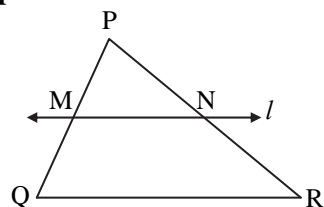




**Converse of Basic Proportionality Theorem:**

**If a line divides any two sides of a triangle in the same ratio, then the line is parallel to the third side.**

If line  $l$  intersects the side  $PQ$  and side  $PR$  of  $\triangle PQR$  in the points  $M$  and  $N$  respectively such that  $\frac{PM}{MQ} = \frac{PN}{NR}$ , then line  $l \parallel$  side  $QR$ .



**Applications of Basic Proportionality Theorem:**

**i. Property of intercepts made by three parallel lines on a transversal:**

**The ratio of the intercepts made on a transversal by three parallel lines is equal to the ratio of the corresponding intercepts made on any other transversal by the same three parallel lines. [3 marks]**

**Given:** line  $l \parallel$  line  $m \parallel$  line  $n$

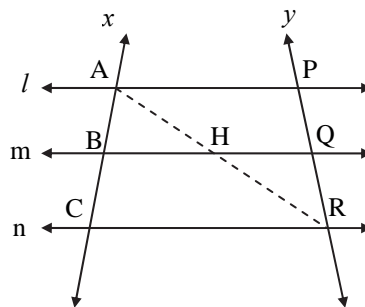
The transversals  $x$  and  $y$  intersect these parallel lines at points  $A, B, C$  and  $P, Q, R$  respectively.

**To Prove that:**  $\frac{AB}{BC} = \frac{PQ}{QR}$

**Construction:** Draw seg  $AR$  to intersect line  $m$  at point  $H$ .

**Proof:**

|  |                           |
|--|---------------------------|
| In $\triangle ACR$ ,                       |                           |
| seg $BH \parallel$ side $CR$               | ---- [Given]              |
| $\therefore \frac{AB}{BC} = \frac{AH}{HR}$ | ---- (i) [By B.P.T.]      |
| In $\triangle ARP$ ,                       |                           |
| seg $HQ \parallel$ side $AP$               | ---- [Given]              |
| $\frac{QR}{PQ} = \frac{RH}{HA}$            | ---- [By B.P.T.]          |
| $\therefore \frac{PQ}{QR} = \frac{AH}{HR}$ | ---- (ii) [By invertendo] |
| $\therefore \frac{AB}{BC} = \frac{PQ}{QR}$ | ---- [From (i) and (ii)]  |



**ii. Property of an angle bisector of a triangle:**

**In a triangle, the angle bisector divides the side opposite to the angle in the ratio of the remaining sides. [Mar 15] [5 marks]**

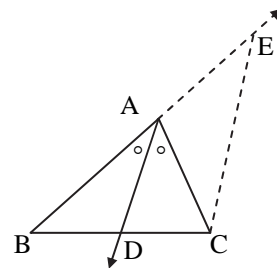
**Given:** In  $\triangle ABC$ , ray  $AD$  bisects  $\angle BAC$

**To Prove that:**  $\frac{BD}{DC} = \frac{AB}{AC}$

**Construction:** Draw a line parallel to ray  $AD$ , passing through point  $C$ .  
Extend  $BA$  to intersect the line at  $E$ .

**Proof:**

|   |  |
|---|--|
| In $\triangle BEC$ ,                                |  |
| seg $AD \parallel$ side $EC$                        | ---- [By construction]                                 |
| $\therefore \frac{BD}{DC} = \frac{AB}{AE}$          | ---- (i) [By B.P.T.]                                   |
| line $AD \parallel$ line $EC$ on transversal $BE$   |  |
| $\therefore \angle BAD \cong \angle AEC$            | ---- (ii) [Corresponding angles]                       |
| line $AD \parallel$ line $EC$ on transversal $AC$ . |  |
| $\therefore \angle CAD \cong \angle ACE$            | ---- (iii) [Alternate angles]                          |
| Also, $\angle BAD \cong \angle CAD$                 | ---- (iv) [ $\because$ Ray $AD$ bisects $\angle BAC$ ] |
| $\therefore \angle AEC \cong \angle ACE$            | ---- (v) [From (ii), (iii) and (iv)]                   |







In  $\triangle AEC$ ,

$$\angle AEC \cong \angle ACE$$

$$\therefore AE = AC$$

$$\therefore \frac{BD}{DC} = \frac{AB}{AC}$$

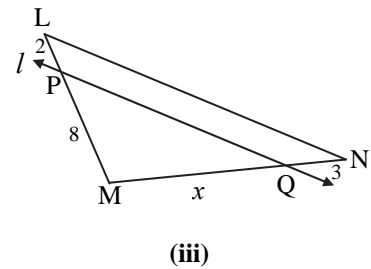
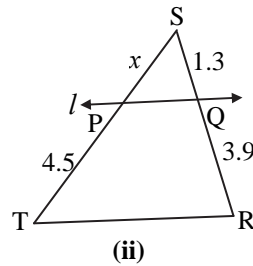
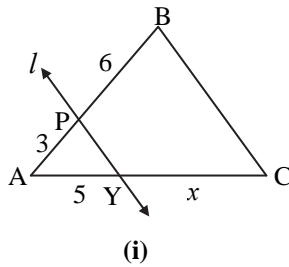
---- [From (v)]

---- (vi) [Sides opposite to congruent angles]

---- [From (i) and (vi)]

### Exercise 1.2

1. Find the values of  $x$  in the following figures, if line  $l$  is parallel to one of the sides of the given triangles.  
[Oct 12, Mar 13] [1 mark each]



**Solution:**

- i. In  $\triangle ABC$ ,  
line  $l \parallel$  side  $BC$

---- [Given]

$$\therefore \frac{AP}{PB} = \frac{AY}{YC}$$

---- [By B.P.T.]

$$\therefore \frac{3}{6} = \frac{5}{x}$$

$$\therefore x = \frac{6 \times 5}{3}$$

$$\therefore x = 10 \text{ units}$$

- ii. In  $\triangle RST$ ,  
line  $l \parallel$  side  $TR$

---- [Given]

$$\frac{SP}{PT} = \frac{SQ}{QR}$$

---- [By B.P.T.]

$$\therefore \frac{x}{4.5} = \frac{1.3}{3.9}$$

$$\therefore x = \frac{1.3 \times 4.5}{3.9}$$

$$\therefore x = \frac{13 \times 45}{39 \times 10}$$

$$\therefore x = 1.5 \text{ units}$$

- iii. In  $\triangle LMN$ ,  
line  $l \parallel$  side  $LN$

---- [Given]

$$\therefore \frac{MP}{PL} = \frac{MQ}{QN}$$

---- [By B.P.T.]

$$\therefore \frac{8}{2} = \frac{x}{3}$$

$$\therefore \frac{3 \times 8}{2} = x$$

$$\therefore x = 3 \times 4$$

$$\therefore x = 12 \text{ units}$$



2. E and F are the points on the side PQ and PR respectively of  $\Delta PQR$ . For each of the following cases, state whether  $EF \parallel QR$ . [2 marks each]

- i.  $PE = 3.9$  cm,  $EQ = 1.3$  cm,  $PF = 3.6$  cm and  $FR = 2.4$  cm.
- ii.  $PE = 4$  cm,  $QE = 4.5$  cm,  $PF = 8$  cm and  $RF = 9$  cm.
- iii.  $PQ = 1.28$  cm,  $PR = 2.56$  cm,  $PE = 0.18$  cm and  $PF = 0.36$  cm.

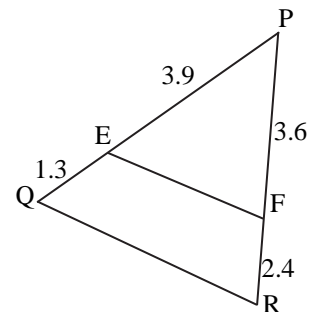
**Solution:**

i.  $\frac{PE}{EQ} = \frac{3.9}{1.3} = \frac{3}{1}$  ---- (i)

$\frac{PF}{FR} = \frac{3.6}{2.4} = \frac{3}{2}$  ---- (ii)

$\therefore$  In  $\Delta PQR$ ,

$\frac{PE}{EQ} \neq \frac{PF}{FR}$  ---- [From (i) and (ii)]



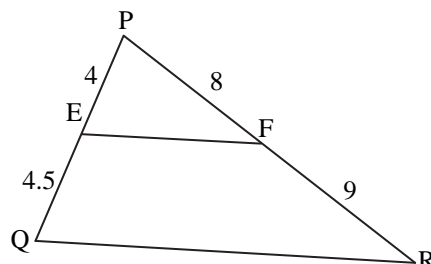
$\therefore$  **seg EF is not parallel to seg QR.**

ii.  $\frac{PE}{QE} = \frac{4}{4.5} = \frac{8}{9}$  ---- (i)

$\frac{PF}{FR} = \frac{8}{9}$  ---- (ii)

In  $\Delta PQR$ ,

$\frac{PE}{QE} = \frac{PF}{FR}$  ---- [From (i) and (ii)]



$\therefore$  **seg EF  $\parallel$  seg QR** ---- [By converse of B.P.T.]

iii.  $EQ + PE = PQ$  ---- [P-E-Q]

$\therefore EQ = PQ - PE$

$= 1.28 - 0.18 = 1.10$

$FR + PF = PR$  ---- [P-F-R]

$\therefore FR = PR - PF$

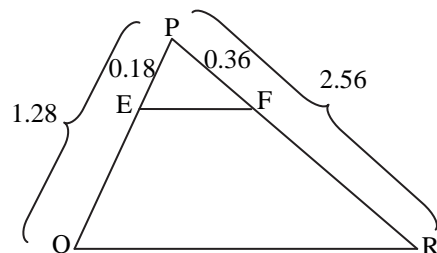
$= 2.56 - 0.36 = 2.20$

$\therefore \frac{PE}{EQ} = \frac{0.18}{1.10} = \frac{18}{110} = \frac{9}{55}$  ---- (i)

$\frac{PF}{FR} = \frac{0.36}{2.20} = \frac{36}{220} = \frac{9}{55}$  ---- (ii)

In  $\Delta PQR$ ,

$\frac{PE}{EQ} = \frac{PF}{FR}$  ---- [From (i) and (ii)]



$\therefore$  **seg EF  $\parallel$  side QR** ---- [By converse of B.P.T.]

3. In the adjoining figure, point Q is on the side MP such that  $MQ = 2$  and  $MP = 5.5$ . Ray NQ is the bisector of  $\angle MNP$  of  $\Delta MNP$ . Find  $MN : NP$ . [2 marks]

**Solution:**

$QP + MQ = MP$  ---- [M-Q-P]

$\therefore QP + 2 = 5.5$

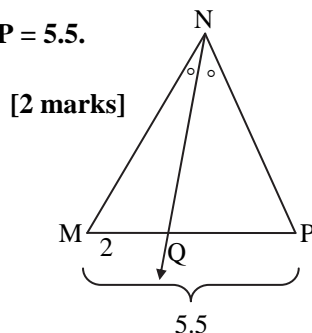
$\therefore QP = 5.5 - 2$

$\therefore QP = 3.5$

In  $\Delta MNP$ ,

ray NQ is the angle bisector of  $\angle MNP$  ---- [Given]

$\therefore \frac{MN}{NP} = \frac{MQ}{QP}$  ---- [By property of angle bisector of a triangle]



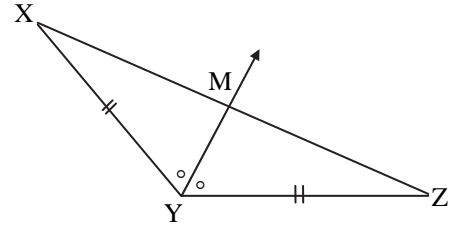


$$\therefore \frac{MN}{NP} = \frac{2}{3.5} = \frac{20}{35} = \frac{4}{7}$$

$$\therefore \frac{MN}{NP} = \frac{4}{7}$$

$$\therefore MN : NP = 4 : 7$$

4. In the adjoining figure, ray YM is the bisector of  $\angle XYZ$ , where  $XY \cong YZ$ . Find the relation between XM and MZ. [2 marks]



**Solution:**

In  $\triangle XYZ$ ,

Ray YM is the angle bisector of  $\angle XYZ$  ---- [Given]

$$\therefore \frac{XM}{MZ} = \frac{XY}{YZ} \text{ ---- (i) [By property of angle bisector of a triangle]}$$

seg  $XY \cong$  seg  $YZ$  ---- [Given]

$$\therefore XY = YZ$$

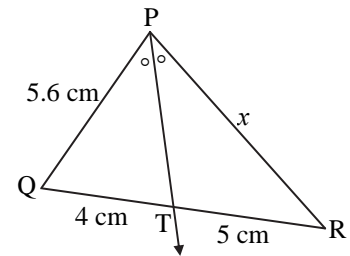
$$\therefore \frac{XY}{YZ} = 1 \text{ ---- (ii)}$$

$$\therefore \frac{XM}{MZ} = 1 \text{ ---- [From (i) and (ii)]}$$

$$\therefore XM = MZ$$

$$\therefore \text{seg } XM \cong \text{seg } MZ$$

5. In the adjoining figure, ray PT is the bisector of  $\angle QPR$ . Find the value of  $x$  and the perimeter of  $\triangle PQR$ . [Mar 14] [3 marks]



**Solution:**

In  $\triangle PQR$ ,

Ray PT is the angle bisector of  $\angle QPR$ .

$$\therefore \frac{PQ}{PR} = \frac{QT}{TR} \text{ ---- [By property of angle bisector of a triangle]}$$

$$\therefore \frac{5.6}{x} = \frac{4}{5}$$

$$\therefore 5.6 \times 5 = 4 \times x$$

$$\therefore \frac{5.6 \times 5}{4} = x$$

$$\therefore x = 7 \text{ cm}$$

$$\therefore PR = 7 \text{ cm} \text{ ---- } [\because PR = x]$$

$$\text{Now, } QR = QT + TR \text{ ---- [Q-T-R]}$$

$$\therefore QR = 4 + 5$$

$$\therefore QR = 9 \text{ cm}$$

$$\begin{aligned} \text{Perimeter of } \triangle PQR &= PQ + QR + PR \\ &= 5.6 + 9 + 7 = 21.6 \text{ cm} \end{aligned}$$

$$\therefore \text{The value of } x \text{ is } 7 \text{ cm and the perimeter of } \triangle PQR \text{ is } 21.6 \text{ cm.}$$

6. In the adjoining figure, if  $ML \parallel BC$  and  $NL \parallel DC$ .

Then prove that  $\frac{AM}{AB} = \frac{AN}{AD}$ . [3 marks]

**Proof:**

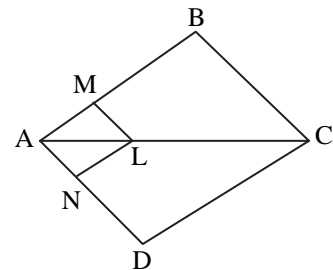
In  $\triangle ABC$ ,

seg  $ML \parallel$  side  $BC$  ---- [Given]

$$\therefore \frac{AM}{MB} = \frac{AL}{LC} \text{ ---- (i) [By B.P.T.]}$$

In  $\triangle ADC$ ,

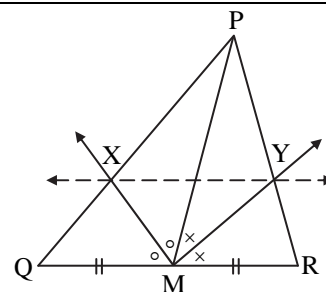
seg  $NL \parallel$  side  $DC$  ---- [Given]





- $\therefore \frac{AN}{ND} = \frac{AL}{LC}$  ----- (ii) [By B.P.T.]  
 $\therefore \frac{AM}{MB} = \frac{AN}{ND}$  ----- [From (i) and (ii)]  
 $\therefore \frac{MB}{AM} = \frac{ND}{AN}$  ----- [By invertendo]  
 $\therefore \frac{MB+AM}{AM} = \frac{ND+AN}{AN}$  ----- [By componendo]  
 $\therefore \frac{AB}{AM} = \frac{AD}{AN}$  ----- [A-M-B, A-N-D]  
 $\therefore \frac{AM}{AB} = \frac{AN}{AD}$  ----- [By invertendo]

7. As shown in the adjoining figure, in  $\Delta PQR$ , seg  $PM$  is the median. Bisectors of  $\angle PMQ$  and  $\angle PMR$  intersect side  $PQ$  and side  $PR$  in points  $X$  and  $Y$  respectively, then prove that  $XY \parallel QR$ . [3 marks]



**Proof:**

Draw line  $XY$ .

In  $\Delta PMQ$ ,

ray  $MX$  is the angle bisector of  $\angle PMQ$ . ----- [Given]

$\therefore \frac{MP}{MQ} = \frac{PX}{QX}$  ----- (i) [By property of angle bisector of a triangle]

In  $\Delta PMR$ ,

ray  $MY$  is the angle bisector of  $\angle PMR$ . ----- [Given]

$\therefore \frac{MP}{MR} = \frac{PY}{RY}$  ----- (ii) [By property of angle bisector of a triangle]

But, seg  $PM$  is the median ----- [Given]

$\therefore M$  is midpoint of seg  $QR$ .

$\therefore MQ = MR$  ----- (iii)

$\therefore \frac{PX}{QX} = \frac{PY}{RY}$  ----- [From (i), (ii) and (iii)]

In  $\Delta PQR$ , seg  $XY \parallel$  seg  $QR$  ----- [By converse of B.P.T.]

8.  $\square ABCD$  is a trapezium in which  $AB \parallel DC$  and its diagonals intersect each other at the point  $O$ .

Show that  $\frac{AO}{BO} = \frac{CO}{DO}$ .

[3 marks]

**Proof:**

$\square ABCD$  is a trapezium.

side  $AB \parallel$  side  $DC$  and seg  $AC$  is a transversal.

$\angle BAC \cong \angle DCA$  ----- (i) [Alternate angles]

In  $\Delta AOB$  and  $\Delta COD$ ,

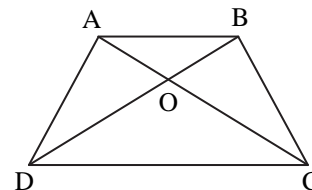
$\angle BAO \cong \angle DCO$  ----- [From (i) and A-O-C]

$\angle AOB \cong \angle COD$  ----- [Vertically opposite angles]

$\therefore \Delta AOB \sim \Delta COD$  ----- [By A-A test of similarity]

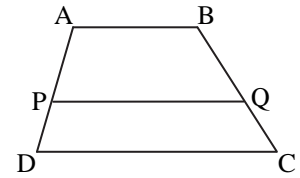
$\therefore \frac{AO}{CO} = \frac{BO}{DO}$  ----- [c.s.s.t.]

$\therefore \frac{AO}{BO} = \frac{CO}{DO}$  ----- [By alternendo]





9. In the adjoining figure,  $\square ABCD$  is a trapezium.  
Side  $AB \parallel$  seg  $PQ \parallel$  side  $DC$  and  $AP = 15$ ,  $PD = 12$ ,  $QC = 14$ , then find  $BQ$ .  
[2 marks]



**Solution:**

Side  $AB \parallel$  seg  $PQ \parallel$  side  $DC$  ---- [Given]

$$\therefore \frac{AP}{PD} = \frac{BQ}{QC} \quad \text{---- [By property of intercepts made by three parallel lines on a transversal]}$$

$$\therefore \frac{15}{12} = \frac{BQ}{14} \quad \text{---- } [\because AP = 15, PD = 12 \text{ and } QC = 14]$$

$$\therefore BQ = \frac{15 \times 14}{12}$$

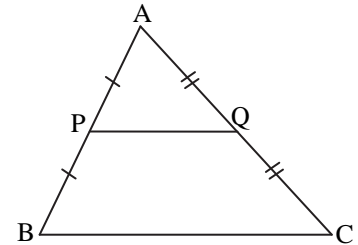
$$\therefore BQ = 17.5$$

10. Using the converse of Basic Proportionality Theorem, prove that the line joining the midpoints of any two sides of a triangle is parallel to the third side and is half of it.  
[4 marks]

**Given:** In  $\triangle ABC$ ,  $P$  and  $Q$  are midpoints of sides  $AB$  and  $AC$  respectively.

**To Prove:** seg  $PQ \parallel$  side  $BC$

$$PQ = \frac{1}{2}BC$$



**Proof:**

$AP = PB$  ---- [P is the midpoint of side AB.]

$$\therefore \frac{AP}{PB} = 1 \quad \text{---- (i)}$$

$AQ = QC$  ---- [Q is the midpoint of side AC.]

$$\therefore \frac{AQ}{QC} = 1 \quad \text{---- (ii)}$$

In  $\triangle ABC$ ,

$$\frac{AP}{PB} = \frac{AQ}{QC} \quad \text{---- [From (i) and (ii)]}$$

$\therefore$  seg  $PQ \parallel$  side  $BC$  ---- (iii) [By converse of B.P.T.]

In  $\triangle ABC$  and  $\triangle APQ$ ,

$\angle ABC \cong \angle APQ$  ---- [From (iii), corresponding angles]

$\angle BAC \cong \angle PAQ$  ---- [Common angle]

$\therefore \triangle ABC \sim \triangle APQ$  ---- [By A-A test of similarity]

$$\therefore \frac{AB}{AP} = \frac{BC}{PQ} \quad \text{---- [c.s.s.t.]}$$

$$\therefore \frac{AP + PB}{AP} = \frac{BC}{PQ} \quad \text{---- [A-P-B]}$$

$$\therefore \frac{AP + AP}{AP} = \frac{BC}{PQ} \quad \text{---- } [\because AP = PB]$$

$$\therefore \frac{2AP}{AP} = \frac{BC}{PQ}$$

$$\therefore \frac{2}{1} = \frac{BC}{PQ}$$

$$\therefore PQ = \frac{1}{2}BC$$





### 1.3 Similarity

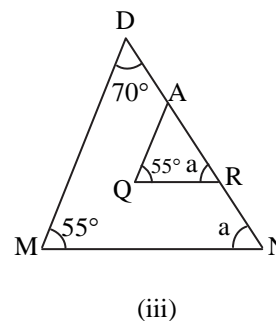
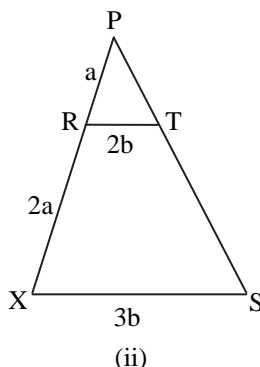
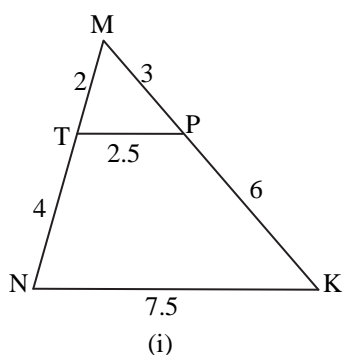
Two figures are called similar if they have same shapes not necessarily the same size.

#### Properties of Similar Triangles:

- Reflexivity:**  $\triangle ABC \sim \triangle ABC$ . It means a triangle is similar to itself.
- Symmetry:** If  $\triangle ABC \sim \triangle DEF$ , then  $\triangle DEF \sim \triangle ABC$ .
- Transitivity:** If  $\triangle ABC \sim \triangle DEF$  and  $\triangle DEF \sim \triangle PQR$ , then  $\triangle PQR \sim \triangle ABC$ .

#### Exercise 1.3

1. Study the following figures and find out in each case whether the triangles are similar. Give reason. [2 marks each]



#### Solution:

- i.  $\triangle MTP$  and  $\triangle MNK$  are similar.

**Reason:**

$$MN = MT + TN \quad \text{---- [M-T-N]}$$

$$\therefore MN = 2 + 4 = 6 \text{ units}$$

$$\therefore \frac{MT}{MN} = \frac{2}{6} = \frac{1}{3} \quad \text{---- (i)}$$

$$MK = MP + PK \quad \text{---- [M-P-K]}$$

$$\therefore MK = 3 + 6 = 9 \text{ units}$$

$$\therefore \frac{MP}{MK} = \frac{3}{9} = \frac{1}{3} \quad \text{---- (ii)}$$

In  $\triangle MTP$  and  $\triangle MNK$ ,

$$\frac{MT}{MN} = \frac{MP}{MK} \quad \text{---- [From (i) and (ii)]}$$

$$\angle TMP \cong \angle NMK \quad \text{---- [Common angle]}$$

$$\therefore \triangle MTP \sim \triangle MNK \quad \text{---- [By S-A-S test of similarity]}$$

- ii.  $\triangle PRT$  and  $\triangle PXS$  are not similar.

**Reason:**

$$PX = PR + RX \quad \text{---- [P-R-X]}$$

$$\therefore PX = a + 2a = 3a$$

$$\therefore \frac{PR}{PX} = \frac{a}{3a} = \frac{1}{3} \quad \text{---- (i)}$$

$$\frac{RT}{XS} = \frac{2b}{3b} = \frac{2}{3} \quad \text{---- (ii)}$$

$$\therefore \frac{PR}{PX} \neq \frac{RT}{XS} \quad \text{---- [From (i) and (ii)]}$$

$\therefore$  The corresponding sides of the two triangles are not in proportion.

$\therefore \triangle PRT$  and  $\triangle PXS$  are not similar.



iii.  $\triangle DMN$  and  $\triangle AQR$  are similar.

**Reason:**

In  $\triangle DMN$  and  $\triangle AQR$ ,

$\angle DMN \cong \angle AQR$  ---- [Each is  $55^\circ$ ]

$\angle DNM \cong \angle ARQ$  ---- [Each is of same measure]

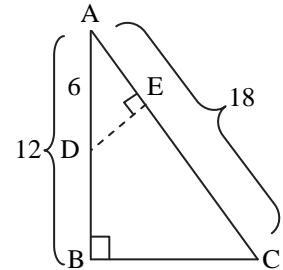
$\therefore \triangle DMN \sim \triangle AQR$  ---- [By A-A test of similarity]

2. In the adjoining figure,  $\triangle ABC$  is right angled at B.

D is any point on AB. seg  $DE \perp$  seg AC.

If  $AD = 6$  cm,  $AB = 12$  cm,  $AC = 18$  cm. Find AE.

[2 marks]



**Solution:**

In  $\triangle AED$  and  $\triangle ABC$ ,

$\angle AED \cong \angle ABC$  ---- [Each is  $90^\circ$ ]

$\angle DAE \cong \angle BAC$  ---- [Common angle]

$\therefore \triangle AED \sim \triangle ABC$  ---- [By A-A test of similarity]

$\therefore \frac{AE}{AB} = \frac{ED}{BC} = \frac{AD}{AC}$  ---- [c.s.s.t.]

$\therefore \frac{AE}{12} = \frac{AD}{18}$

$\therefore \frac{AE}{12} = \frac{6}{18}$

$\therefore AE = \frac{6 \times 12}{18}$

$\therefore AE = 4$  cm

3. In the adjoining figure, E is a point on side CB produced of an isosceles

$\triangle ABC$  with  $AB = AC$ . If  $AD \perp BC$  and  $EF \perp AC$ ,

prove that  $\triangle ABD \sim \triangle ECF$ .

[3 marks]

**Proof:**

In  $\triangle ABC$ ,

seg  $AB \cong$  seg  $AC$  ---- [Given]

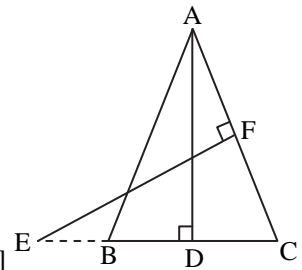
$\angle B \cong \angle C$  ---- (i) [By isosceles triangle theorem]

In  $\triangle ABD$  and  $\triangle ECF$ ,

$\angle ABD \cong \angle ECF$  ---- [From (i)]

$\angle ADB \cong \angle EFC$  ---- [Each is  $90^\circ$ ]

$\therefore \triangle ABD \sim \triangle ECF$  ---- [By A-A test of similarity]



4. D is a point on side BC of  $\triangle ABC$  such that  $\angle ADC = \angle BAC$ . Show that  $AC^2 = BC \times DC$ . [3 marks]

**Proof:**

In  $\triangle ACB$  and  $\triangle DCA$ ,

$\angle BAC \cong \angle ADC$  ---- [Given]

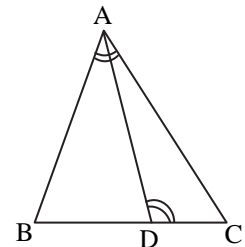
$\angle ACB \cong \angle DCA$  ---- [Common angle]

$\therefore \triangle ACB \sim \triangle DCA$  ---- [By A-A test of similarity]

$\therefore \frac{AC}{DC} = \frac{BC}{AC} = \frac{AB}{DA}$  ---- [c.s.s.t.]

$\therefore \frac{AC}{DC} = \frac{BC}{AC}$

$\therefore AC^2 = BC \times DC$





5. A vertical pole of length 6 m casts a shadow of 4 m long on the ground. At the same time, a tower casts a shadow 28 m long. Find the height of the tower. [3 marks]

**Solution:**

AB represents the length of the pole.

$$\therefore AB = 6 \text{ m}$$

BC represents the shadow of the pole.

$$\therefore BC = 4 \text{ m}$$

PQ represents the height of the tower.

QR represents the shadow of the tower.

$$\therefore QR = 28 \text{ m}$$

$$\Delta ABC \sim \Delta PQR$$

---- [ $\because$  vertical pole and tower are similar figures]

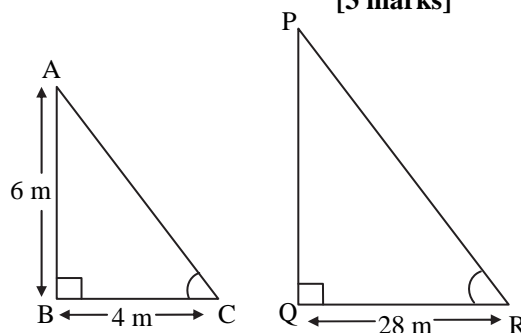
$$\therefore \frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR} \quad \text{---- [c.s.s.t.]}$$

$$\therefore \frac{AB}{PQ} = \frac{BC}{QR} \quad \therefore \frac{6}{PQ} = \frac{4}{28}$$

$$\therefore \frac{6}{PQ} = \frac{1}{7} \quad \therefore 6 \times 7 = PQ$$

$$\therefore PQ = 42 \text{ m}$$

$\therefore$  **Height of the tower is 42 m.**



6. Triangle ABC has sides of length 5, 6 and 7 units while  $\Delta PQR$  has perimeter of 360 units. If  $\Delta ABC$  is similar to  $\Delta PQR$ , then find the sides of  $\Delta PQR$ . [3 marks]

**Solution:**

Since,  $\Delta ABC \sim \Delta PQR$

$$\therefore \frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR} \quad \text{---- [c.s.s.t.]}$$

$$\therefore \frac{5}{PQ} = \frac{6}{QR} = \frac{7}{PR}$$

By theorem on equal ratios,

$$\text{each ratio} = \frac{5+6+7}{PQ+QR+PR}$$

$$= \frac{18}{360}$$

$$= \frac{1}{20}$$

---- [ $\because$  Perimeter of  $\Delta PQR = PQ + QR + PR = 360$ ]

$$\therefore \frac{5}{PQ} = \frac{6}{QR} = \frac{7}{PR} = \frac{1}{20} \quad \text{---- (i)}$$

$$\frac{5}{PQ} = \frac{1}{20}$$

---- [From (i)]

$$\therefore PQ = 20 \times 5$$

$$\therefore PQ = 100 \text{ units}$$

$$\frac{6}{QR} = \frac{1}{20}$$

---- [From (i)]

$$\therefore QR = 6 \times 20$$

$$\therefore QR = 120 \text{ units}$$

$$\frac{7}{PR} = \frac{1}{20}$$

---- [From (i)]

$$\therefore PR = 7 \times 20$$

$$\therefore PR = 140 \text{ units}$$

$\therefore$   **$\Delta PQR$  has sides PQ, QR and PR of length 100 units, 120 units and 140 units respectively.**

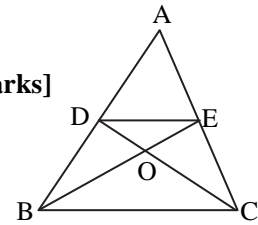


$$\begin{aligned} \text{iii. } \frac{A(\Delta PBC)}{A(\Delta PQA)} &= \frac{25}{1} && \text{---- [By invertendo]} \\ \therefore \frac{A(\Delta PBC) - A(\Delta PQA)}{A(\Delta PQA)} &= \frac{25-1}{1} && \text{---- [By dividendo]} \\ \therefore \frac{A(\square QBCA)}{A(\Delta PQA)} &= \frac{24}{1} \\ \therefore \frac{A(\square PQA)}{A(\square QBCA)} &= \frac{1}{24} && \text{---- [By invertendo]} \\ \therefore A(\Delta PQA) : A(\square QBCA) &= 1 : 24 \end{aligned}$$

7. In the adjoining figure,  $DE \parallel BC$  and  $AD : DB = 5 : 4$ .

Find: i.  $DE : BC$       ii.  $DO : DC$       iii.  $A(\Delta DOE) : A(\Delta DCE)$

[5 marks]



**Solution:**

$$\begin{aligned} \text{i. } DE \parallel BC &&& \text{---- [Given]} \\ AB \text{ is a transversal} &&& \\ \therefore \angle ADE \cong \angle ABC &&& \text{---- (i) [Corresponding angles]} \\ \text{In } \Delta ADE \text{ and } \Delta ABC, &&& \\ \angle ADE \cong \angle ABC &&& \text{---- [From (i)]} \\ \angle DAE \cong \angle BAC &&& \text{---- [Common angle]} \\ \therefore \Delta ADE \sim \Delta ABC &&& \text{---- [By A-A test of similarity]} \\ \therefore \frac{AD}{AB} = \frac{DE}{BC} &&& \text{---- (ii) [c.s.s.t.]} \\ \frac{AD}{DB+AD} = \frac{5}{4+5} &&& \text{---- [Substituting the given values]} \\ \therefore \frac{AD}{DB+AD} = \frac{5}{9} &&& \text{---- [By invertendo]} \\ \therefore \frac{DB+AD}{AD} = \frac{4+5}{5} &&& \text{---- [By componendo]} \\ \therefore \frac{AB}{AD} = \frac{9}{5} &&& \text{---- [A-D-B]} \\ \therefore \frac{AD}{AB} = \frac{5}{9} &&& \text{---- (iii) [By invertendo]} \\ \therefore \frac{DE}{BC} = \frac{5}{9} &&& \text{---- (iv) [From (ii) and (iii)]} \\ \therefore DE : BC = 5 : 9 \end{aligned}$$

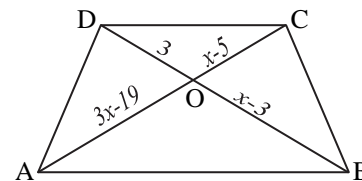

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$$\begin{aligned} \text{ii. } \text{In } \Delta DOE \text{ and } \Delta COB, &&& \\ \angle EDO \cong \angle BCO &&& \text{---- [Alternate angles on parallel lines DE and BC]} \\ \angle DOE \cong \angle COB &&& \text{---- [Vertically opposite angles]} \\ \therefore \Delta DOE \sim \Delta COB &&& \text{---- [By A-A test of similarity]} \\ \therefore \frac{DO}{OC} = \frac{DE}{BC} &&& \text{---- [c.s.s.t.]} \\ \therefore \frac{DO}{OC} = \frac{5}{9} &&& \text{---- [From (iv)]} \\ \therefore \frac{OC}{DO} = \frac{9}{5} &&& \text{---- [By invertendo]} \\ \therefore \frac{OC+DO}{DO} = \frac{9+5}{5} &&& \text{---- [By componendo]} \\ \therefore \frac{DC}{DO} = \frac{14}{5} &&& \text{---- [D-O-C]} \\ \therefore \frac{DO}{DC} = \frac{5}{14} &&& \text{---- (v) [By invertendo]} \\ \therefore DO : DC = 5 : 14 \end{aligned}$$



- iii.  $\frac{A(\triangle DOE)}{A(\triangle DCE)} = \frac{DO}{DC}$  ---- [Ratio of areas of two triangles having equal heights is equal to the ratio of the corresponding bases]
- $\therefore \frac{A(\triangle DOE)}{A(\triangle DCE)} = \frac{5}{14}$  ---- [From (v)]
- $\therefore A(\triangle DOE) : A(\triangle DCE) = 5 : 14$

8. In the adjoining figure, seg AB || seg DC.  
Using the information given, find the value of x. [3 marks]

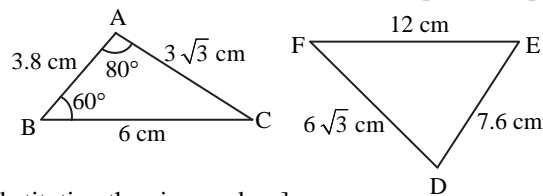


**Solution:**

Side DC || Side AB on transversal DB.

- $\therefore \angle ABD \cong \angle CDB$  ---- (i) [Alternate angles]
- In  $\triangle AOB$  and  $\triangle COD$ ,
- $\angle ABO \cong \angle CDO$  ---- [From (i), D – O – B]
- $\angle AOB \cong \angle COD$  ---- [Vertically opposite angles]
- $\therefore \triangle AOB \sim \triangle COD$  ---- [By A–A test of similarity]
- $\therefore \frac{OA}{OC} = \frac{OB}{OD}$  ---- [c.s.s.t]
- $\therefore \frac{3x-19}{x-5} = \frac{x-3}{3}$  ---- [Substituting the given values]
- $\therefore 3(3x-19) = (x-3)(x-5)$
- $\therefore 9x-57 = x^2-8x+15$
- $\therefore x^2-8x-9x+15+57=0$
- $\therefore x^2-17x+72=0$
- $\therefore (x-9)(x-8)=0$
- $\therefore x-9=0$  or  $x-8=0$
- $\therefore x=9$  or  $x=8$

9. Using the information given in the adjoining figure, find  $\angle F$ . [3 marks]



**Solution:**

- $\frac{AB}{DE} = \frac{3.8}{12} = \frac{1}{2}$  ---- (i)
- $\frac{BC}{EF} = \frac{6}{12} = \frac{1}{2}$  ---- (ii)
- $\frac{CA}{FD} = \frac{3\sqrt{3}}{6\sqrt{3}} = \frac{1}{2}$  ---- (iii)
- In  $\triangle ABC$  and  $\triangle DEF$ ,
- $\therefore \frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$  ---- [From (i), (ii) and (iii)]
- $\therefore \triangle ABC \sim \triangle DEF$  ---- [By S–S–S test of similarity]
- $\angle C \cong \angle F$  ---- (iv) [c.a.s.t]
- In  $\triangle ABC$ ,
- $\angle A + \angle B + \angle C = 180^\circ$  ---- [Sum of the measures of all angles of a triangle is  $180^\circ$ .]
- $\therefore 80^\circ + 60^\circ + \angle C = 180^\circ$  ---- [Substituting the given values]
- $\therefore \angle C = 180^\circ - 140^\circ$
- $\therefore \angle C = 40^\circ$  ---- (v)
- $\therefore \angle F = 40^\circ$  ---- [From (iv) and (v)]





10. A vertical stick 12 m long casts a shadow 8 m long on the ground. At the same time a tower casts the shadow of length 40 m on the ground. Determine the height of the tower. [2 marks]

**Solution:**

Let AB represent the vertical stick, AB = 12 m.

BC represents the shadow of the stick, BC = 8 m.

PQ represents the height of the tower.

QR represents the shadow of the tower, QR = 40 m.

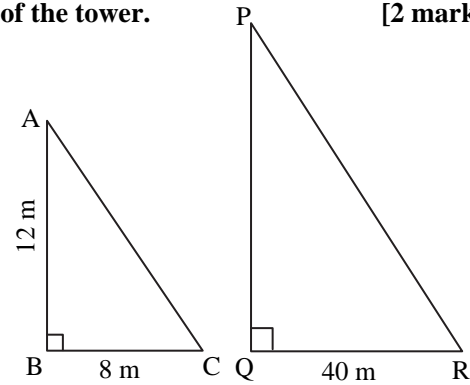
$\triangle ABC \sim \triangle PQR$

$$\therefore \frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR} \quad \text{---- [c.s.s.t.]}$$

$$\therefore \frac{12}{PQ} = \frac{8}{40} \quad \text{---- [Substituting the given values]}$$

$$\therefore PQ = 12 \times 5 = 60$$

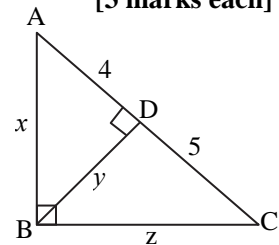
$\therefore$  The height of the tower is 60 m.



11. In each of the figures, an altitude is drawn to the hypotenuse. The lengths of different segments are marked in each figure. Determine the value of  $x$ ,  $y$ ,  $z$  in each case. [3 marks each]

**Solution:**

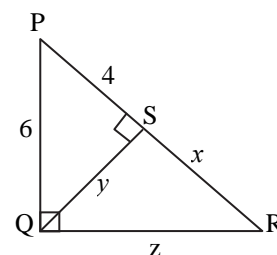
- i. In  $\triangle ABC$ ,  $m\angle ABC = 90^\circ$  ---- [Given]  
 seg  $BD \perp$  hypotenuse  $AC$  ---- [Given]  
 $\therefore BD^2 = AD \times DC$  ---- [By property of geometric mean]  
 $\therefore y^2 = 4 \times 5$  ---- [Substituting the given values]  
 $\therefore y = \sqrt{4 \times 5}$  ---- [Taking square root on both sides]  
 $\therefore y = 2\sqrt{5}$  ---- (i)



- In  $\triangle ADB$ ,  
 $m\angle ADB = 90^\circ$  ---- [ $\because$  Seg  $BD \perp$  hypotenuse  $AC$ ]  
 $AB^2 = AD^2 + BD^2$  ---- [By Pythagoras theorem]  
 $\therefore x^2 = (4)^2 + y^2$  ---- [Substituting the given values]  
 $\therefore x^2 = 4^2 + (2\sqrt{5})^2$  ---- [From (i)]  
 $\therefore x^2 = 16 + 20$   
 $\therefore x^2 = 36$   
 $\therefore x = 6$  ---- [Taking square root on both sides]  
 In  $\triangle BDC$ ,  
 $m\angle BDC = 90^\circ$  ---- [ $\because$  Seg  $BD \perp$  hypotenuse  $AC$ ]  
 $\therefore BC^2 = BD^2 + CD^2$  ---- [By Pythagoras theorem]  
 $\therefore z^2 = y^2 + (5)^2$  ---- [Substituting the given values]  
 $\therefore z^2 = (2\sqrt{5})^2 + (5)^2$  ---- [From (i)]  
 $\therefore z^2 = 20 + 25$   
 $\therefore z^2 = 45$   
 $\therefore z = \sqrt{9 \times 5}$  ---- [Taking square root on both sides]  
 $\therefore z = 3\sqrt{5}$   
 $\therefore x = 6, y = 2\sqrt{5}$  and  $z = 3\sqrt{5}$



ii. In  $\Delta PSQ$ ,  
 $m \angle PSQ = 90^\circ$  ---- [ $\because$  Seg QS  $\perp$  hypotenuse PR]  
 $\therefore PQ^2 = PS^2 + QS^2$  ---- [By Pythagoras theorem]  
 $\therefore (6)^2 = (4)^2 + y^2$  ---- [Substituting the given values]  
 $\therefore 36 = 16 + y^2$   
 $\therefore y^2 = 36 - 16$   
 $\therefore y^2 = 20$   
 $\therefore y = \sqrt{4 \times 5}$  ---- [Taking square root on both sides]  
 $\therefore y = 2\sqrt{5}$  ---- (i)  
 In  $\Delta PQR$ ,  
 seg QS  $\perp$  hypotenuse PR ---- [Given]  
 $\therefore QS^2 = PS \times SR$  ---- [By the property of geometric mean]  
 $\therefore y^2 = 4 \times x$  ---- [Substituting the given values]  
 $\therefore (2\sqrt{5})^2 = 4x$  ---- [From (i)]  
 $\therefore 20 = 4x$   
 $\therefore x = \frac{20}{4}$   
 $\therefore x = 5$  ---- (ii)  
 In  $\Delta QSR$ ,  
 $m \angle QSR = 90^\circ$  ---- [ $\because$  Seg QS  $\perp$  hypotenuse PR]  
 $\therefore QR^2 = QS^2 + SR^2$  ---- [By Pythagoras theorem]  
 $\therefore z^2 = y^2 + x^2$  ---- [Substituting the given values]  
 $\therefore z^2 = (2\sqrt{5})^2 + (5)^2$  ---- [From (i) and (ii)]  
 $\therefore z^2 = 20 + 25$   
 $\therefore z^2 = 45$   
 $\therefore z = \sqrt{9 \times 5}$  ---- [Taking square root on both sides]  
 $\therefore z = 3\sqrt{5}$   
 $\therefore x = 5, y = 2\sqrt{5}$  and  $z = 3\sqrt{5}$

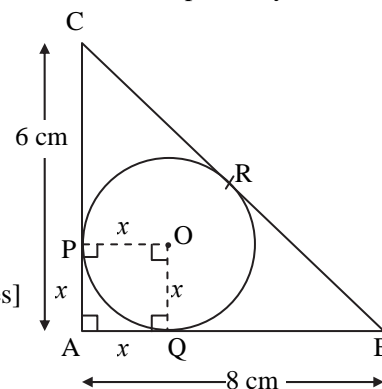


12.  $\Delta ABC$  is a right angled triangle with  $\angle A = 90^\circ$ . A circle is inscribed in it. The lengths of the sides containing the right angle are 6 cm and 8 cm. Find the radius of the circle. [4 marks]

**Construction:** Let P, Q and R be the points of contact of tangents AC, AB and BC respectively and draw segments OP and OQ.

**Solution:**

In  $\Delta ABC$ ,  
 $\angle BAC = 90^\circ$  ---- [Given]  
 $\therefore BC^2 = AC^2 + AB^2$  ---- [By Pythagoras theorem]  
 $\therefore BC^2 = (6)^2 + (8)^2$  ---- [Substituting the given values]  
 $\therefore BC^2 = 36 + 64$   
 $\therefore BC^2 = 100$   
 $\therefore BC = 10$  units ---- (i) [Taking square root on both sides]  
 Let the radius of the circle be  $x$  cm.  
 $\therefore OP = OQ = x$  ---- [Radii of same circle]  
 In  $\square OPAQ$ ,  
 $\angle OPA = \angle OQA = 90^\circ$  ---- [Radius is  $\perp$  to the tangent]  
 $\angle PAQ = 90^\circ$  ---- [Given]  
 $\therefore \angle POQ = 90^\circ$  ---- [Remaining angle]  
 $\therefore \square OPAQ$  is a rectangle ---- [By definition]  
 But,  $OP = OQ$  ---- [Radii of same circle]  
 $\therefore \square OPAQ$  is a square ---- [A rectangle is a square if its adjacent sides are congruent]  
 $\therefore OP = OQ = QA = AP = x$  ---- [Sides of a square]





Now,  $AQ + BQ = AB$   
 $\therefore x + BQ = 8$   
 $\therefore BQ = 8 - x$   
 $AP + CP = AC$   
 $\therefore x + CP = 6$   
 $\therefore CP = 6 - x$   
 $BQ = BR = 8 - x$   
 $CP = CR = 6 - x$   
 $BC = CR + BR$   
 $\therefore 10 = 6 - x + 8 - x$   
 $\therefore 2x = 4$   
 $\therefore x = 2$   
 $\therefore$  **The radius of the circle is 2 cm.**

---- [A–Q–B]  
 ---- [Substituting the given values]  
 ---- [A–P–C]  
 ---- [Substituting the given values]  
 ---- (ii) } [Length of tangent segments drawn from an external point  
 ---- (iii) } to the circle are equal.]  
 ---- (iv) [C–R–B]  
 ---- [From (i), (ii), (iii) and (iv)]

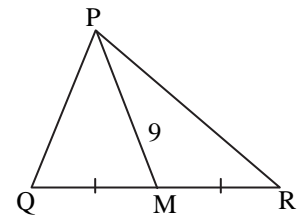
13. In  $\Delta PQR$ , seg  $PM$  is a median. If  $PM = 9$  and  $PQ^2 + PR^2 = 290$ , find  $QR$ .

[2 marks]

**Solution:**

In  $\Delta PQR$ ,  
 seg  $PM$  is the median  
 $\therefore PQ^2 + PR^2 = 2PM^2 + 2MR^2$   
 $\therefore 290 = 2(9)^2 + 2MR^2$   
 $\therefore 290 = 2(81) + 2MR^2$   
 $\therefore 290 = 162 + 2MR^2$   
 $\therefore 2MR^2 = 290 - 162$   
 $\therefore 2MR^2 = 128$   
 $\therefore MR^2 = \frac{128}{2}$   
 $\therefore MR^2 = 64$   
 $\therefore MR = 8$   
 Also,  $QR = 2MR$   
 $\therefore QR = 2 \times 8$   
 $\therefore QR = 16$

---- [Given]  
 ---- [By Apollonius theorem]  
 ---- [Substituting the given values]  
 ---- (i) [Taking square root on both sides]  
 ---- [ $\because$  M is the midpoint of seg QR]  
 ---- [From (i)]



14. From the information given in the adjoining figure,

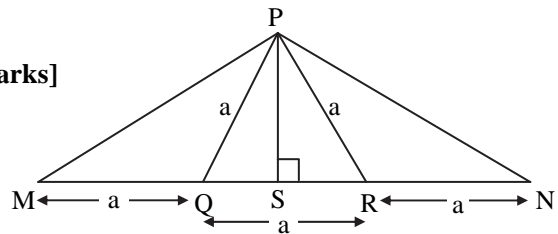
Prove that:  $PM = PN = \sqrt{3} \times a$ , where  $QR = a$ . [4 marks]

**Proof:**

In  $\Delta PMR$ ,  
 $QM = QR = a$   
 $\therefore$  Q is midpoint of seg  $MR$ .  
 $\therefore$  seg  $PQ$  is the median  
 $\therefore PM^2 + PR^2 = 2PQ^2 + 2QM^2$   
 $\therefore PM^2 + a^2 = 2a^2 + 2a^2$   
 $\therefore PM^2 + a^2 = 4a^2$   
 $\therefore PM^2 = 3a^2$   
 $\therefore PM = \sqrt{3}a$

Similarly, we can prove  
 $PN = \sqrt{3}a$   
 $\therefore PM = PN = \sqrt{3}a$

---- [Given]  
 ---- [By Apollonius theorem]  
 ---- [Substituting the given values]  
 ---- [Taking square root on both sides]

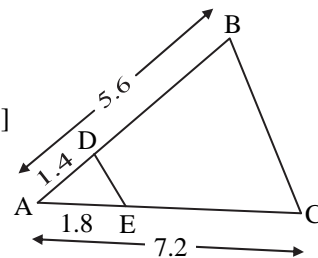




15. D and E are the points on sides AB and AC such that  $AB = 5.6$ ,  $AD = 1.4$ ,  $AC = 7.2$  and  $AE = 1.8$ . Show that  $DE \parallel BC$ . [2 marks]

**Proof:**

$DB = AB - AD$  ----- [A-D-B]  
 $\therefore DB = 5.6 - 1.4$  ----- [Substituting the given values]  
 $\therefore DB = 4.2$  units  
 $\therefore \frac{AD}{DB} = \frac{1.4}{4.2} = \frac{1}{3}$  ----- (i)  
 Also,  $EC = AC - AE$  ----- [A-E-C]  
 $\therefore EC = 7.2 - 1.8$  ----- [Substituting the given values]  
 $\therefore EC = 5.4$  units  
 $\therefore \frac{AE}{EC} = \frac{1.8}{5.4} = \frac{1}{3}$  ----- (ii)  
 In  $\triangle ABC$ ,  
 $\frac{AD}{DB} = \frac{AE}{EC}$  ----- [From (i) and (ii)]  
 $\therefore \text{seg } DE \parallel \text{seg } BC$  ----- [By converse of B.P.T.]



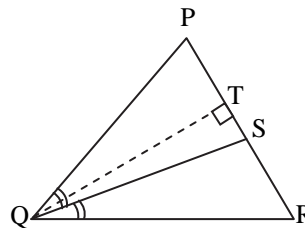
16. In  $\triangle PQR$ , if  $QS$  is the angle bisector of  $\angle Q$ , then show that

$$\frac{A(\triangle PQS)}{A(\triangle QRS)} = \frac{PQ}{QR} \quad \text{[3 marks]}$$

(Hint: Draw  $QT \perp PR$ )

**Proof:**

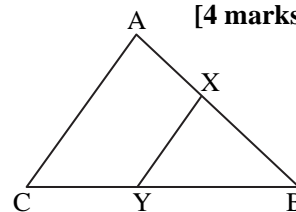
In  $\triangle PQR$ ,  
 Ray  $QS$  is the angle bisector of  $\angle PQR$  ----- [Given]  
 $\therefore \frac{PQ}{QR} = \frac{PS}{SR}$  ----- (i) [By property of angle bisector of a triangle]  
 Height of  $\triangle PQS = \text{Height of } \triangle QRS = QT$   
 $\therefore \frac{A(\triangle PQS)}{A(\triangle QRS)} = \frac{PS}{SR}$  ----- (ii) [Ratio of areas of two triangles having equal heights is equal to the ratio of their corresponding bases]  
 $\therefore \frac{A(\triangle PQS)}{A(\triangle QRS)} = \frac{PQ}{QR}$  ----- [From (i) and (ii)]



17. In the adjoining figure,  $XY \parallel AC$  and  $XY$  divides the triangular region  $ABC$  into two equal areas. Determine  $AX : AB$ . [4 marks]

**Solution:**

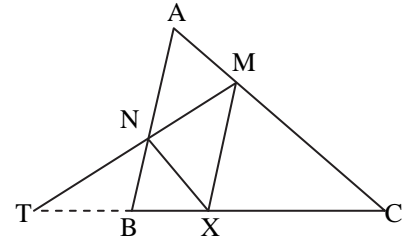
seg  $XY \parallel$  side  $AC$  on transversal  $BC$   
 $\angle XYB \cong \angle ACB$  ----- (i) [Corresponding angles]  
 In  $\triangle XYB$  and  $\triangle ACB$ ,  
 $\angle XYB \cong \angle ACB$  ----- [From (i)]  
 $\angle XBY \cong \angle CBY$  ----- [Common angle]  
 $\therefore \triangle XYB \sim \triangle ACB$  ----- [By A-A test of similarity]  
 $\frac{A(\triangle XYB)}{A(\triangle ACB)} = \frac{XB^2}{AB^2}$  ----- (ii) [By theorem on areas of similar triangles]  
 Now,  $A(\triangle XYB) = \frac{1}{2} A(\triangle ACB)$  ----- [ $\because$  seg  $XY$  divides the triangular region  $ABC$  into two equal areas]  
 $\therefore \frac{A(\triangle XYB)}{A(\triangle ACB)} = \frac{1}{2}$  ----- (iii)  
 $\therefore \frac{XB^2}{AB^2} = \frac{1}{2}$  ----- [From (ii) and (iii)]  
 $\therefore \frac{XB}{AB} = \frac{1}{\sqrt{2}}$  ----- [Taking square root on both sides]





$$\begin{aligned} \therefore 1 - \frac{XB}{AB} &= 1 - \frac{1}{\sqrt{2}} && \text{---- [Subtracting both sides from 1]} \\ \therefore \frac{AB - XB}{AB} &= \frac{\sqrt{2} - 1}{\sqrt{2}} \\ \therefore \frac{AX}{AB} &= \frac{\sqrt{2} - 1}{\sqrt{2}} && \text{---- [A-X-B]} \\ \therefore \mathbf{AX : AB} &= (\sqrt{2} - 1) : \sqrt{2} \end{aligned}$$

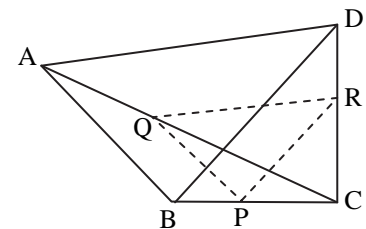
18. Let X be any point on side BC of  $\triangle ABC$ , XM and XN are drawn parallel to BA and CA. MN meets produced BC in T. Prove that  $TX^2 = TB \cdot TC$ . [4 marks]



**Proof:**

$$\begin{aligned} &\text{In } \triangle TXM, \\ &\text{seg } BN \parallel \text{seg } XM && \text{---- [Given]} \\ \therefore \frac{TN}{NM} &= \frac{TB}{BX} && \text{---- (i) [By B.P.T.]} \\ &\text{In } \triangle TMC, \\ &\text{seg } XN \parallel \text{seg } CM && \text{---- [Given]} \\ \therefore \frac{TN}{NM} &= \frac{TX}{CX} && \text{---- (ii) [By B.P.T.]} \\ \therefore \frac{TB}{BX} &= \frac{TX}{CX} && \text{---- [From (i) and (ii)]} \\ \therefore \frac{BX}{TB} &= \frac{CX}{TX} && \text{---- [By invertendo]} \\ \therefore \frac{BX + TB}{TB} &= \frac{CX + TX}{TX} && \text{---- [By componendo]} \\ \therefore \frac{TX}{TB} &= \frac{TC}{TX} && \text{---- [T-B-X, T-X-C]} \\ \therefore \mathbf{TX^2} &= \mathbf{TB \cdot TC} \end{aligned}$$

19. Two triangles,  $\triangle ABC$  and  $\triangle DBC$ , lie on the same side of the base BC. From a point P on BC,  $PQ \parallel AB$  and  $PR \parallel BD$  are drawn. They intersect AC at Q and DC at R. They



Prove that  $QR \parallel AD$ . [3 marks]

**Proof:**

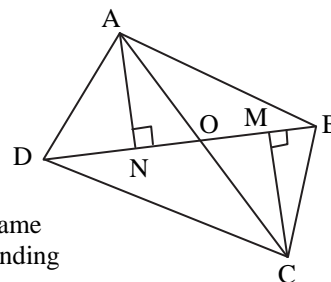
$$\begin{aligned} &\text{In } \triangle CAB, \\ &\text{seg } PQ \parallel \text{seg } AB && \text{---- [Given]} \\ \therefore \frac{CP}{PB} &= \frac{CQ}{AQ} && \text{---- (i) [By B.P.T.]} \\ &\text{In } \triangle CBD, \\ &\text{seg } PR \parallel \text{seg } BD && \text{---- [Given]} \\ \therefore \frac{CP}{PB} &= \frac{CR}{RD} && \text{---- (ii) [By B.P.T.]} \\ &\text{In } \triangle ACD, \\ \therefore \frac{CQ}{AQ} &= \frac{CR}{RD} && \text{---- [From (i) and (ii)]} \\ \therefore \mathbf{\text{seg } QR} &\parallel \mathbf{\text{seg } AD} && \text{---- [By converse of B.P.T.]} \end{aligned}$$



20. In the figure,  $\triangle ADB$  and  $\triangle CDB$  are on the same base  $DB$ .

If  $AC$  and  $BD$  intersect at  $O$ , then prove that  $\frac{A(\triangle ADB)}{A(\triangle CDB)} = \frac{AO}{CO}$

[3 marks]



**Proof:**

$$\frac{A(\triangle ADB)}{A(\triangle CDB)} = \frac{AN}{CM}$$

----(i) [Ratio of areas of two triangles with the same base is equal to the ratio of their corresponding heights]

In  $\triangle ANO$  and  $\triangle CMO$ ,

$$\angle ANO \cong \angle CMO$$

---- [Each is  $90^\circ$ ]

$$\angle AON \cong \angle COM$$

---- [Vertically opposite angles]

$$\therefore \triangle ANO \sim \triangle CMO$$

---- [By A-A test of similarity]

$$\therefore \frac{AN}{CM} = \frac{AO}{CO}$$

---- (ii) [c.s.s.t.]

$$\therefore \frac{A(\triangle ADB)}{A(\triangle CDB)} = \frac{AO}{CO}$$

---- [From (i) and (ii)]

21. In  $\triangle ABC$ ,  $D$  is a point on  $BC$  such that  $\frac{BD}{DC} = \frac{AB}{AC}$ . Prove that  $AD$  is the bisector of  $\angle A$ .

(Hint: Produce  $BA$  to  $E$  such that  $AE = AC$ . Join  $EC$ )

[5 marks]

**Proof:**

seg  $BA$  is produced to point  $E$  such that  $AE = AC$  and seg  $EC$  is drawn.

$$\frac{BD}{DC} = \frac{AB}{AC}$$

---- (i) [Given]

$$AC = AE$$

---- (ii) [By construction]

$$\therefore \frac{BD}{DC} = \frac{AB}{AE}$$

---- (iii) [Substituting (ii) in (i)]

$$\therefore \text{seg } AD \parallel \text{seg } EC$$

---- [By converse of B.P.T.]

On transversal  $BE$ ,

$$\angle BAD \cong \angle BEC$$

---- [Corresponding angles]

$$\therefore \angle BAD \cong \angle AEC$$

---- (iv) [ $\because B - A - E$ ]

On transversal  $AC$ ,

$$\angle CAD \cong \angle ACE$$

---- (v) [Alternate angles]

In  $\triangle ACE$ ,

$$\text{seg } AC \cong \text{seg } AE$$

---- [By construction]

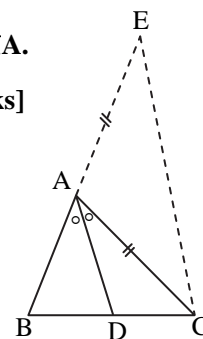
$$\angle AEC \cong \angle ACE$$

---- (vi) [By isosceles triangle theorem]

$$\therefore \angle BAD \cong \angle CAD$$

---- [From (iv), (v) and (vi)]

$\therefore$  Ray  $AD$  is the bisector of  $\angle BAC$

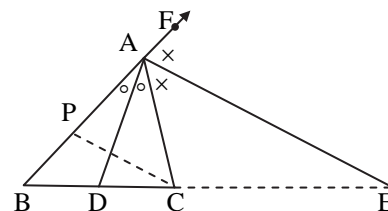


22. The bisector of interior  $\angle A$  of  $\triangle ABC$  meets  $BC$  in  $D$ . The bisector of exterior  $\angle A$  meets  $BC$  produced in  $E$ . Prove that

$$\frac{BD}{BE} = \frac{CD}{CE}$$

(Hint: For the bisector of  $\angle A$  which is exterior of  $\triangle ABC$ ,  $\frac{AB}{AC} = \frac{BE}{CE}$ )

[5 marks]



**Construction:** Draw seg  $CP \parallel$  seg  $AE$  meeting  $AB$  at point  $P$ .

**Proof:**

In  $\triangle ABC$ ,

Ray  $AD$  is bisector of  $\angle BAC$

---- [Given]

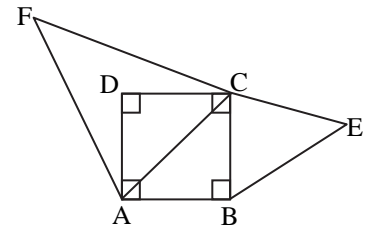
$$\therefore \frac{AB}{AC} = \frac{BD}{CD}$$

---- (i) [By property of angle bisector of triangle]



- In  $\triangle ABE$ ,  
 seg  $CP \parallel$  seg  $AE$  ---- [By construction]  
 $\therefore \frac{BC}{CE} = \frac{BP}{AP}$  ---- [B. P. T]  
 $\frac{BC+CE}{CE} = \frac{BP+AP}{AP}$  ---- [By componendo]  
 $\therefore \frac{BE}{CE} = \frac{AB}{AP}$  ---- (ii)  
 seg  $CP \parallel$  seg  $AE$  on transversal  $BF$ .  
 $\angle FAE \cong \angle APC$  ---- (iii) [Corresponding angles]  
 seg  $CP \parallel$  seg  $AE$  on transversal  $AC$ .  
 $\angle CAE \cong \angle ACP$  ---- (iv) [Alternate angles]  
 Also,  $\angle FAE \cong \angle CAE$  ---- (v) [Seg  $AE$  bisects  $\angle FAC$ ]  
 $\therefore \angle APC \cong \angle ACP$  ---- (vi) [From (iii), (iv) and (v)]  
 In  $\triangle APC$ ,  
 $\angle APC \cong \angle ACP$  ---- [From (vi)]  
 $\therefore AP = AC$  ---- (vii) [By converse of isosceles triangle theorem]  
 $\therefore \frac{BE}{CE} = \frac{AB}{AC}$  ---- (viii) [From (ii) and (vii)]  
 $\therefore \frac{BD}{CD} = \frac{BE}{CE}$  ---- [From (i) and (viii)]  
 $\therefore \frac{BD}{BE} = \frac{CD}{CE}$  ---- [By alternendo]

23. In the adjoining figure,  $\square ABCD$  is a square.  $\triangle BCE$  on side  $BC$  and  $\triangle ACF$  on the diagonal  $AC$  are similar to each other. Then, show that  $A(\triangle BCE) = \frac{1}{2} A(\triangle ACF)$ . [3 marks]



**Proof:**

- $\square ABCD$  is a square. ---- [Given]  
 $\therefore AC = \sqrt{2} BC$  ---- (i) [ $\because$  Diagonal of a square =  $\sqrt{2} \times$  side of square]  
 $\triangle BCE \sim \triangle ACF$  ---- [Given]  
 $\therefore \frac{A(\triangle BCE)}{A(\triangle ACF)} = \frac{(BC)^2}{(AC)^2}$  ---- (ii) [By theorem on areas of similar triangles]  
 $\therefore \frac{A(\triangle BCE)}{A(\triangle ACF)} = \frac{(BC)^2}{(\sqrt{2} \cdot BC)^2}$  ---- [From (i) and (ii)]  
 $\therefore \frac{A(\triangle BCE)}{A(\triangle ACF)} = \frac{BC^2}{2BC^2}$   
 $\therefore \frac{A(\triangle BCE)}{A(\triangle ACF)} = \frac{1}{2}$   
 $\therefore A(\triangle BCE) = \frac{1}{2} A(\triangle ACF)$

24. Two poles of height 'a' meters and 'b' metres are 'p' meters apart. Prove that the height 'h' drawn from the point of intersection N of the lines joining the top of each pole to the foot of the opposite pole is  $\frac{ab}{a+b}$  metres. [4 marks]

**Proof:**

Let  $RT = x$  and  $TQ = y$ .

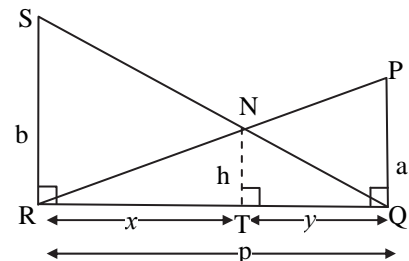
In  $\triangle PQR$  and  $\triangle NTR$ ,

$\angle PQR \cong \angle NTR$

$\angle PRQ \cong \angle NRT$

---- [Each is  $90^\circ$ ]

---- [Common angle]

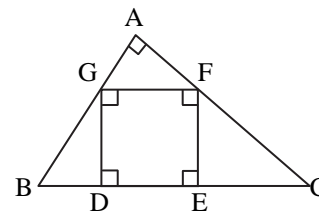




$\therefore \Delta PQR \sim \Delta NTR$  ---- [By A – A test of similarity]  
 $\therefore \frac{PQ}{NT} = \frac{QR}{TR}$  ---- [c.s.s.t.]  
 $\therefore \frac{a}{h} = \frac{p}{x}$  ---- [Substituting the given values]  
 $\therefore x = \frac{ph}{a}$  ---- (i)  
 In  $\Delta SRQ$  and  $\Delta NTQ$ ,  
 $\angle SRQ \cong \angle NTQ$  ---- [Each is  $90^\circ$ ]  
 $\angle SQR \cong \angle NQT$  ---- [Common angle]  
 $\Delta SRQ \sim \Delta NTQ$  ---- [By A–A test of similarity]  
 $\therefore \frac{SR}{NT} = \frac{QR}{QT}$  ---- [c.s.s.t.]  
 $\therefore \frac{b}{h} = \frac{p}{y}$  ---- [Substituting the given values]  
 $\therefore y = \frac{ph}{b}$  ---- (ii)  
 $x + y = \frac{ph}{a} + \frac{ph}{b}$  ---- [Adding (i) and (ii)]  
 $\therefore p = ph \left( \frac{1}{a} + \frac{1}{b} \right)$  ---- [R – T – Q]  
 $\therefore \frac{p}{ph} = \frac{b+a}{ab}$   
 $\therefore \frac{1}{h} = \frac{a+b}{ab}$   
 $\therefore h = \frac{ab}{a+b}$  metres ---- [By invertendo]

25. In the adjoining figure,  $\square DEFG$  is a square and  $\angle BAC = 90^\circ$ .

- Prove that: i.  $\Delta AGF \sim \Delta DBG$  ii.  $\Delta AGF \sim \Delta EFC$   
 iii.  $\Delta DBG \sim \Delta EFC$  iv.  $DE^2 = BD \cdot EC$   
 [5 marks]



**Proof:**

i.  $\square DEFG$  is a square. ---- [Given]  
 seg  $GF \parallel$  seg  $DE$  ---- [Opposite sides of a square]  
 $\therefore$  seg  $GF \parallel$  seg  $BC$  ---- (i) [B–D–E–C]  
 In  $\Delta AGF$  and  $\Delta DBG$ ,  
 $\angle GAF \cong \angle BDG$  ---- [Each is  $90^\circ$ ]  
 $\angle AGF \cong \angle DBG$  ---- [Corresponding angles of parallel lines  $GF$  and  $BC$ ]  
 $\therefore \Delta AGF \sim \Delta DBG$  ---- (ii) [By A–A test of similarity]

---

ii. In  $\Delta AGF$  and  $\Delta EFC$ ,  
 $\angle GAF \cong \angle FEC$  ---- [Each is  $90^\circ$ ]  
 $\angle AFG \cong \angle ECF$  ---- [Corresponding angles of parallel lines  $GF$  and  $BC$ ]  
 $\therefore \Delta AGF \sim \Delta EFC$  ---- (iii) [By A–A test of similarity]

---

iii. Since,  $\Delta AGF \sim \Delta DBG$  ---- [From (ii)]  
 and  $\Delta AGF \sim \Delta EFC$  ---- [From (iii)]  
 $\therefore \Delta DBG \sim \Delta EFC$  ---- [From (ii) and (iii)]





iv. Since,  $\triangle DBG \sim \triangle EFC$

$$\frac{BD}{FE} = \frac{DG}{EC} \quad \text{---- [c.s.s.t.]}$$

$$\therefore DG \times FE = BD \times EC \quad \text{---- (iv)}$$

$$\text{But, } DG = EF = DE \quad \text{---- (v) [Sides of a square]}$$

$$\therefore DE \times DE = DB \times EC \quad \text{---- [From (iv) and (v)]}$$

$$\therefore DE^2 = BD \cdot EC$$

### One-Mark Questions

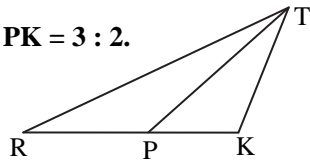
1. In  $\triangle ABC$  and  $\triangle XYZ$ ,  $\frac{AB}{YZ} = \frac{BC}{ZX} = \frac{AC}{XY}$ , then state by which correspondence are  $\triangle ABC$  and  $\triangle XYZ$  similar.

**Solution:**

$\triangle ABC \sim \triangle XYZ$  by  $ABC \leftrightarrow YZX$ .

2. In the figure,  $RP : PK = 3 : 2$ .

$$\text{Find } \frac{A(\triangle TRP)}{A(\triangle TPK)}.$$



**Solution:**

Ratio of the areas of two triangles having equal heights is equal to the ratio of their corresponding bases.

$$\therefore \frac{A(\triangle TRP)}{A(\triangle TPK)} = \frac{RP}{PK} = \frac{3}{2}$$

3. Write the statement of Basic Proportionality Theorem.

**Solution:**

If a line parallel to a side of a triangle intersects the other sides in two distinct points, then the line divides those sides in proportion.

4. What is the ratio among the length of the sides of any triangle of angles  $30^\circ - 60^\circ - 90^\circ$ ?

**Solution:**

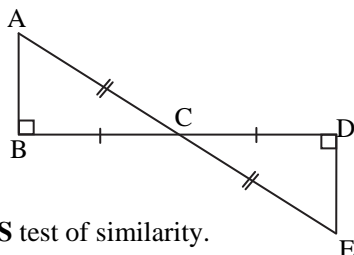
The ratio is  $1 : \sqrt{3} : 2$ .

5. What is the ratio among the length of the sides of any triangle of angles  $45^\circ - 45^\circ - 90^\circ$ ?

**Solution:**

The ratio is  $1 : 1 : \sqrt{2}$ .

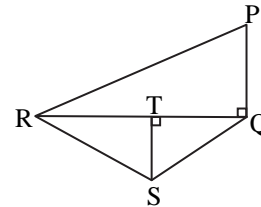
6. State the test by which the given triangles are similar.



**Solution:**

$\triangle ABC \sim \triangle EDC$  by SAS test of similarity.

7. In the adjoining figure, find  $\frac{A(\triangle PQR)}{A(\triangle RSQ)}$ .



**Solution:**

Ratio of the areas of two triangles having equal bases is equal to the ratio of their corresponding heights.

$$\therefore \frac{A(\triangle PQR)}{A(\triangle RSQ)} = \frac{PQ}{ST}$$

8. Find the diagonal of a square whose side is 10 cm. [Mar 15]

**Solution:**

Diagonal of a square =  $\sqrt{2} \times \text{side}$ .

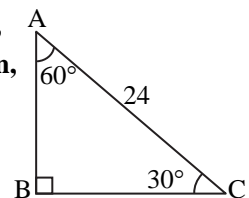
$$= \sqrt{2} \times (10) = 10\sqrt{2} \text{ cm}$$

9. Adjacent sides of parallelogram are 11 cm and 17 cm respectively. If length of one diagonal is 26 cm, then using which theorem/property can we find the length of the other diagonal?

**Solution:**

We can find the length of the other diagonal by using Apollonius' theorem.

10. In the adjoining figure, using given information, find BC.



**Solution:**

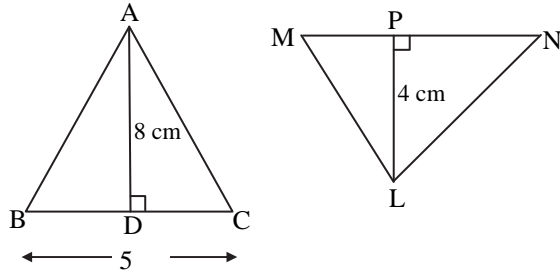
$$BC = \frac{\sqrt{3}}{2} \times AC \quad \text{---- [Side opposite to } 60^\circ \text{]}$$

$$= \frac{\sqrt{3}}{2} \times 24$$

$$\therefore BC = 12\sqrt{3} \text{ units}$$



11. Find the value of MN, so that  $A(\triangle ABC) = A(\triangle LMN)$ .



**Solution:**

$$A(\triangle ABC) = A(\triangle LMN)$$

$$\therefore \frac{1}{2} \times BC \times AD = \frac{1}{2} \times MN \times LP$$

$$\therefore \frac{1}{2} \times 5 \times 8 = \frac{1}{2} \times MN \times 4$$

$$\therefore MN = \frac{5 \times 8}{4}$$

$$\therefore MN = 10 \text{ cm}$$

12. If the sides of a triangle are 6 cm, 8 cm and 10 cm respectively, determine whether the triangle is right angled triangle or not. [Mar 14]

**Solution:**

Note that,  
 $6^2 + 8^2 = 10^2$ ,

$\therefore$  By converse of Pythagoras theorem, the given triangle is a right angled triangle.

13. Sides of the triangle are 7 cm, 24 cm and 25 cm. Determine whether the triangle is right-angled triangle or not. [Oct 14]

**Solution:**

The longest side is 25 cm.

$$\therefore (25)^2 = 625 \quad \dots(i)$$

Now, sum of the squares of the other two sides will be

$$(7)^2 + (24)^2 = 49 + 576 = 625 \quad \dots(ii)$$

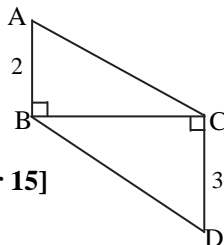
$$\therefore (25)^2 = (7)^2 + (24)^2 \quad \dots[\text{From (i) and (ii)}]$$

Yes, the given sides form a right angled triangle.

$\dots$ [By converse of Pythagoras theorem]

14. In the following figure seg AB  $\perp$  seg BC, seg DC  $\perp$  seg BC. If AB = 2 and DC = 3,

find  $\frac{A(\triangle ABC)}{A(\triangle DCB)}$ . [Mar 15]



**Solution:**

Ratio of the areas of two triangles having equal base is equal to the ratio of their corresponding heights.

$$\therefore \frac{A(\triangle ABC)}{A(\triangle DCB)} = \frac{AB}{DC} \quad \therefore \frac{A(\triangle ABC)}{A(\triangle DCB)} = \frac{2}{3}$$

15. Find the diagonal of a square whose side is 16 cm. [July 15]

**Solution:**

$$\begin{aligned} \text{Diagonal of a square} &= \sqrt{2} \times \text{side.} \\ &= \sqrt{2} \times 16 = 16\sqrt{2} \text{ cm} \end{aligned}$$

### Additional Problems for Practice

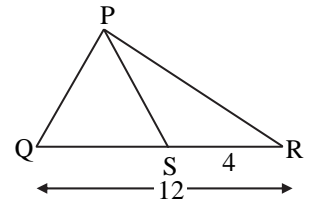
#### Based on Exercise 1.1

1. In the adjoining figure, QR = 12 and SR = 4. Find values of

i.  $\frac{A(\triangle PSR)}{A(\triangle PQR)}$

ii.  $\frac{A(\triangle PQS)}{A(\triangle PQR)}$

iii.  $\frac{A(\triangle PQS)}{A(\triangle PSR)}$



[3 marks]

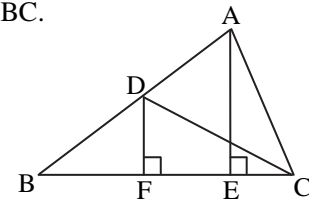
2. The ratio of the areas of two triangles with the equal heights is 3 : 4. Base of the smaller triangle is 15 cm. Find the corresponding base of the larger triangle. [2 marks]

3. In the adjoining figure, seg AE  $\perp$  seg BC and seg DF  $\perp$  seg BC. Find

i.  $\frac{A(\triangle ABC)}{A(\triangle DBC)}$

ii.  $\frac{A(\triangle DBF)}{A(\triangle DFC)}$

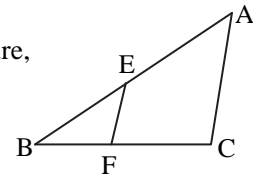
iii.  $\frac{A(\triangle AEC)}{A(\triangle DBF)}$



[2 marks]

#### Based on Exercise 1.2

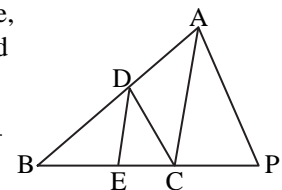
4. In the adjoining figure, seg EF  $\parallel$  side AC, AB = 18, AE = 10, BF = 4. Find BC.



[3 marks]

5. In the adjoining figure, seg DE  $\parallel$  side AC and seg DC  $\parallel$  side AP.

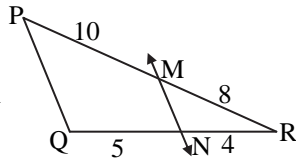
Prove that  $\frac{BE}{EC} = \frac{BC}{CP}$



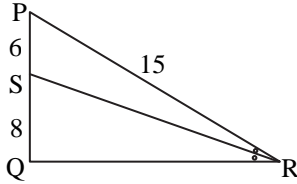
[3 marks]



6. In the adjoining figure,  $PM = 10$ ,  $MR = 8$ ,  $QN = 5$ ,  $NR = 4$ . State with reason whether line  $MN$  is parallel to side  $PQ$  or not? [2 marks]

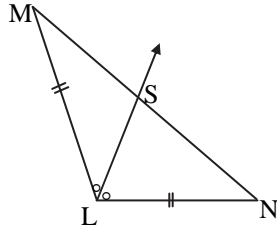


7. In the following figure, in a  $\Delta PQR$ , seg  $RS$  is the bisector of  $\angle PRQ$ ,  $PS = 6$ ,  $SQ = 8$ ,  $PR = 15$ . Find  $QR$ . [Mar 15][2 marks]

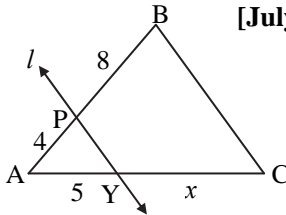


8. Bisectors of  $\angle B$  and  $\angle C$  in  $\Delta ABC$  meet each other at  $P$ . Line  $AP$  cuts the side  $BC$  at  $Q$ . Then prove that  $\frac{AP}{PQ} = \frac{AB+AC}{BC}$ . [3 marks]

9. In the figure given below Ray  $LS$  is the bisector of  $\angle MLN$ , where seg  $ML \cong$  seg  $LN$ , find the relation between  $MS$  and  $SN$ . [3 marks]

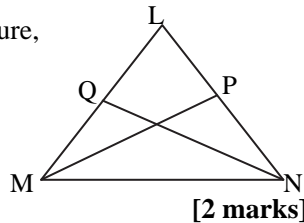


10. In the given figure, line  $l \parallel$  side  $BC$ ,  $AP = 4$ ,  $PB = 8$ ,  $AY = 5$  and  $YC = x$ . Find  $x$ . [July 15] [2 marks]

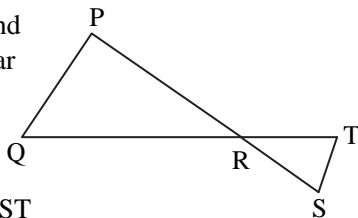


## Based on Exercise 1.3

11. In the adjoining figure,  $\Delta MPL \sim \Delta NQL$ ,  $MP = 21$ ,  $ML = 35$ ,  $NQ = 18$ ,  $QL = 24$ . Find  $PL$  and  $NL$ . [2 marks]



12. In the adjoining figure,  $\Delta PQR$  and  $\Delta RST$  are similar under  $PQR \leftrightarrow STR$ ,  $PQ = 12$ ,  $PR = 15$ ,  $\frac{QR}{TR} = \frac{3}{2}$ . Find  $ST$  and  $SR$ . [2 marks]

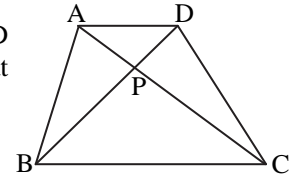


13. In the map of a triangular field, sides are shown by 8 cm, 7 cm and 6 cm. If the largest side of the triangular field is 400 m, find the remaining sides of the field. [3 marks]

14.  $\Delta EFG \sim \Delta RST$  and  $EF = 8$ ,  $FG = 10$ ,  $EG = 6$ ,  $RS = 4$ . Find  $ST$  and  $RT$ . [2 marks]

15. In  $\square ABCD$ , side  $BC \parallel$  side  $AD$ . [Oct 09] [4 marks]

Diagonals  $AC$  and  $BD$  intersect each other at  $P$ .



If  $AP = \frac{1}{3}AC$ , then

prove that  $DP = \frac{1}{2}BP$ .

## Based on Exercise 1.4

16. If  $\Delta PQR \sim \Delta PMN$  and

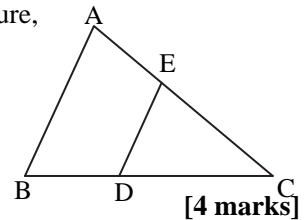
$9A(\Delta PQR) = 6A(\Delta PMN)$ , then find  $\frac{QR}{MN}$ . [2 marks]

17.  $\Delta LMN \sim \Delta RST$  and  $A(\Delta LMN) = 100$  sq. cm,  $A(\Delta RST) = 144$  sq. cm,  $LM = 5$  cm. Find  $RS$ . [2 marks]

18.  $\Delta ABC$  and  $\Delta DEF$  are equilateral triangles.  $A(\Delta ABC) : A(\Delta DEF) = 1 : 2$  and  $AB = 4$  cm. Find  $DE$ . [2 marks]

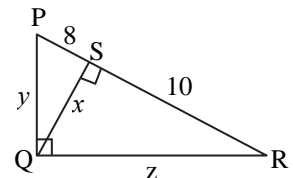
19. If the areas of two similar triangles are equal, then prove that they are congruent. [4 marks]

20. In the adjoining figure, seg  $DE \parallel$  side  $AB$ ,  $DC = 2BD$ ,  $A(\Delta CDE) = 20$  cm<sup>2</sup>. Find  $A(\square ABDE)$ . [4 marks]

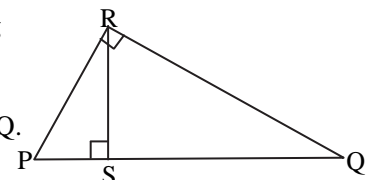


## Based on Exercise 1.5

21. In the adjoining figure,  $\angle PQR = 90^\circ$ , seg  $QS \perp$  side  $PR$ . Find values of  $x$ ,  $y$  and  $z$ . [3 marks]

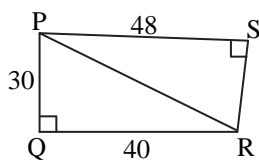


22. In the adjoining figure,  $\angle PRQ = 90^\circ$ , seg  $RS \perp$  seg  $PQ$ . Prove that :  $\frac{PR^2}{QR^2} = \frac{PS}{QS}$  [3 marks]



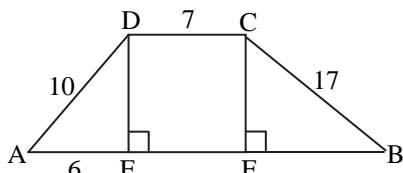


23. In the adjoining figure,  
 $\angle PQR = 90^\circ$ ,  
 $\angle PSR = 90^\circ$ .



Find:  
 i. PR and ii. RS [3 marks]

24. In the adjoining figure,  
 $\square ABCD$  is a trapezium, seg  $AB \parallel$  seg  $DC$ ,  
 seg  $DE \perp$  side  $AB$ , seg  $CF \perp$  side  $AB$ .

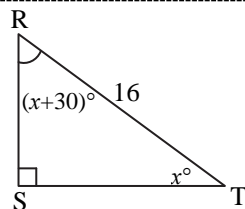


Find: i. DE and CF ii. BF  
 iii. AB. [5 marks]

25. Starting from Anil's house, Peter first goes 50 m to south, then 75 m to west, then 62 m to North and finally 40 m to east and reaches Salim's house. Then find the distance between Anil's house and Salim's house. [5 marks]

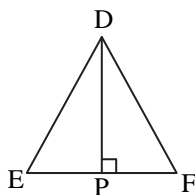
**Based on Exercise 1.6**

26. In the adjoining figure,  
 $\angle S = 90^\circ$ ,  $\angle T = x^\circ$ ,  
 $\angle R = (x + 30)^\circ$ ,  
 $RT = 16$ .



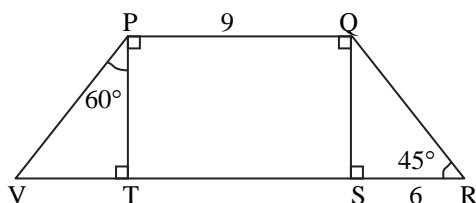
Find: i. RS  
 ii. ST [3 marks]

27.  $\triangle DEF$  is an equilateral triangle.  
 seg  $DP \perp$  side  $EF$ ,  
 and  $E-P-F$ .



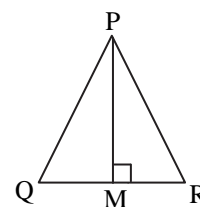
Prove that :  
 $DP^2 = 3 EP^2$   
 [Oct 08] [4 marks]

28. In the adjoining figure,  
 $\square PQRV$  is a trapezium, seg  $PQ \parallel$  seg  $VR$ .  
 $SR = 6$ ,  $PQ = 9$ , Find  $VR$ .



[Mar 13] [3 marks]

29. In the adjoining figure,  $\triangle PQR$  is an equilateral triangle,  
 seg  $PM \perp$  side  $QR$ .  
 Prove that:  
 $PQ^2 = 4QM^2$



[3 marks]

**Based on Exercise 1.7**

30. In  $\triangle PQR$ , seg  $PM$  is a median.  $PM = 10$  and  $PQ^2 + PR^2 = 362$ . Find  $QR$ . [2 marks]
31. Adjacent sides of a parallelogram are 11 cm and 17 cm. Its one diagonal is 12 cm. Find its other diagonal. [4 marks]
32. In  $\triangle ABC$ ,  $\angle ABC = 90^\circ$ ,  $AB = 12$ ,  $BC = 16$  and seg  $BP$  is a median. Find  $BP$ . [3 marks]

**Answers to additional problems for practice**

1. i.  $\frac{1}{3}$  ii.  $\frac{2}{3}$  iii.  $\frac{2}{1}$
2. 20 cm
3. i.  $\frac{AE}{DF}$  ii.  $\frac{BF}{FC}$   
 iii.  $\frac{EC \times AE}{BF \times DF}$
4. 9 units
6. Yes, line  $MN \parallel$  side  $PQ$
7. 20 units
9. seg  $MS \cong$  seg  $SN$
10. 10 unit
11.  $PL = 28$  units and  $NL = 30$  units
12.  $ST = 8$  units and  $SR = 10$  units
13. Remaining sides of field are 350 m and 300 m.
14.  $ST = 5$  units and  $RT = 3$  units
16.  $\frac{4}{3}$
17. 6 cm
18.  $4\sqrt{2}$  cm
20.  $25 \text{ cm}^2$
21.  $x = 4\sqrt{5}$  units,  $y = 12$  units and  $z = 6\sqrt{5}$  units
23. i. 50 units ii. 14 units
24. i.  $DE = 8$  units and  $CF = 8$  units  
 ii.  $BF = 15$  units  
 iii.  $AB = 28$  units
25. 37 m
26. i. 8 units ii.  $8\sqrt{3}$  units
28.  $(15 + 6\sqrt{3})$  units
30. 18 units
31. 26 cm
32. 10 units